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Technical Note

No. 60

Boulder Laboratories

AMPLITUDE AND PHASE OF THE LOW- AND VERY-LOW- RADIOFREQUENCY GROUND WAVE

BY J.R. JOHLER, L.C. WALTERS, AND C.M. LILLEY



U. S. DEPARTMENT OF COMMERCE
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June 1, 1960

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AMPLITUDE AND PHASE OF THE LOW- AND VERY LOW-RADIOFREQUENCY GROUND WAVE

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ABSTRACT

Graphs and tables of the low- and very low-radiofrequency ground wave are presented as a function of frequency, 100 c/s to 1000 kc.

PREFACE

Computation techniques for the classical Bremmer-van der Pol theory have been developed¹. As a result of various theoretical ground wave pulse investigations during the past several years with the aid of electronic computer programs, a considerable volume of calculated data on the ground wave has been accumulated and is

1

J. R. Johler, W. J. Kellar, L. C. Walters, "Phase of the Low-Radiofrequency Ground Wave," NBS Circular 573, U. S. Gov. Print. Off., Washington, D. C., (1956). See also, J. R. Johler, L. C. Walters, C. M. Lilley, "Low- and Very Low-Radiofrequency Tables of Ground Wave Parameters for the Spherical Earth Theory: The Roots of Riccati's Differential Equation," NBS Technical Note No. 7, PB 151366, February 1, 1959. An extensive bibliography is presented in the above papers. The following paper is of interest in the LF-VLF spectrum: J. R. Wait and H. H. Howe, "Amplitude and Phase Curves for Ground Wave Propagation in the Band 200 Cycles per Second to 500 Kilocycles," NBS Circular 574, U. S. Gov. Print. Off., Washington, D. C. (1956).

herewith presented in tabular and graphical form². The computer program employed the techniques described in NBS Circular 573, hence, the formulas will not be repeated here. The amplitude, $|E_r|$ volts/meter and the phase $\arg E_r = \phi_c$, radians have been tabulated for various frequencies, f , distances, d , conductivities σ , dielectric constants ϵ_2 , and vertical lapse of permittivity factors α . The tables employ standard tabular frequencies, f , and Gaussian frequencies, f_m , described in published work on pulse propagation³. All fields, $|E_r|$, are normalized to a standard dipole current mount, $I_o l = 1$. With the aid of the expression⁴,

$$P_r = 1.6 (10^{-13}) \omega^2 (I_o l)^2 / z_o ,$$

²

This tabulation was motivated by USAF Ground Electronics Engineering and Installation Agency (GEEIA) requirements of NBS project 8570-40-85472 and the application of the ground wave theory to LF radio navigation systems such as Loran-C (Cyctac) system described in the following publication: W. P. Frantz, W. Dean, R. L. Frank, "A Precision Multipurpose Radio Navigation System," IRE 1957 Convention Record, Part 8, pp. 79-102.

³

See for example, J. R. Johler and L. C. Walters, "Propagation of a Ground Wave Pulse Around a Finitely Conducting Spherical Earth from a Damped Sinusoidal Source Current," IRE Trans. on antennas and propagation, Vol. AP-7, No. 1, January 1959, pp. 1-10.

⁴

The notion of radiated power, P_r , is apparently due to S. Ballantine, "On the Radiation Resistance of a Simple Vertical Antenna at Wavelengths Below the Fundamental," Proc, IRE Vol. 12, December 1924, pp. 823-839.

where $z_0 = 377$ ohms, the conventional engineering notion of radiated power, P_r , can be introduced. It is only necessary to employ a linear translation of the scale, $|E_r|$ volts/meter for dipole current moments other than unity. These considerations, of course, do not affect the phase.

The phase $\arg E_r = \phi_c$ is tabulated in radians. These values can be readily converted to the conventional radio navigation system microseconds, t_c ,

$$t_c = 10^6 \phi_c / \omega .$$

The table entries include a number and an associated power of ten (10). The integers to the right of each table entry, if present, indicates the power of the factor ten (10) by which the entry is to be multiplied, thus, for example, $6.4307-1 = 0.64307$.

The number of terms $(s + 1)$, $s = 0, 1, 2, 3 \dots$, of the series of residues required for the calculation can be estimated with the aid of Figs. 1, 2, assuming eight significant figure precision. Of course, if less computation precision is required, fewer terms are necessary. Note the large increase in the number of terms required at short distances and low frequencies as a result of the slow convergence of the series of residues.

Boulder, Colorado, June 1, 1960.

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<u>Fig.</u>	<u>σ</u>	<u>ϵ_2</u>	<u>α</u>	<u>f, kc</u>	<u>d, mi</u>	
3	0.0005	15	0.85	0.01-1000	5000-50	7
4	0.002	15	0.85	0.01-1000	5000-50	8
5	0.005	15	0.85	0.01-1000	5000-50	9
6	0.0005	15	0.85	0.01-1000	12, 49, 329, 621, 1000	10
7	0.002	15	0.85	0.01-1000	12.49, 329, 621, 1000	11
8	5	80	0.85	0.01-1000	12.49, 329, 621, 1000	12

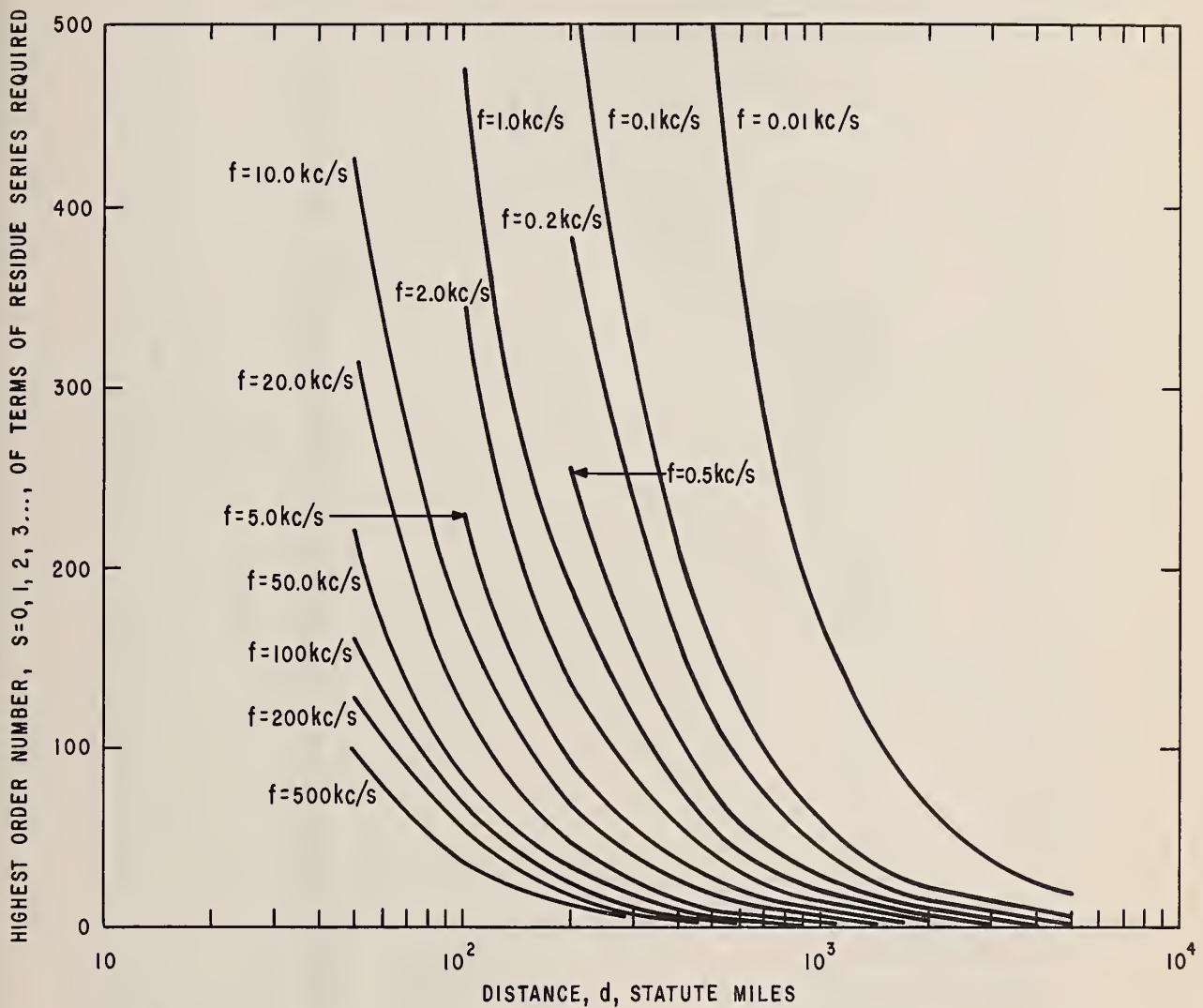


Fig. 1 - Highest order number, $s = 0, 1, 2, 3\dots$, of terms of the series of residues required for eight significant figure computation precision as a function of distance from the source for various frequencies.

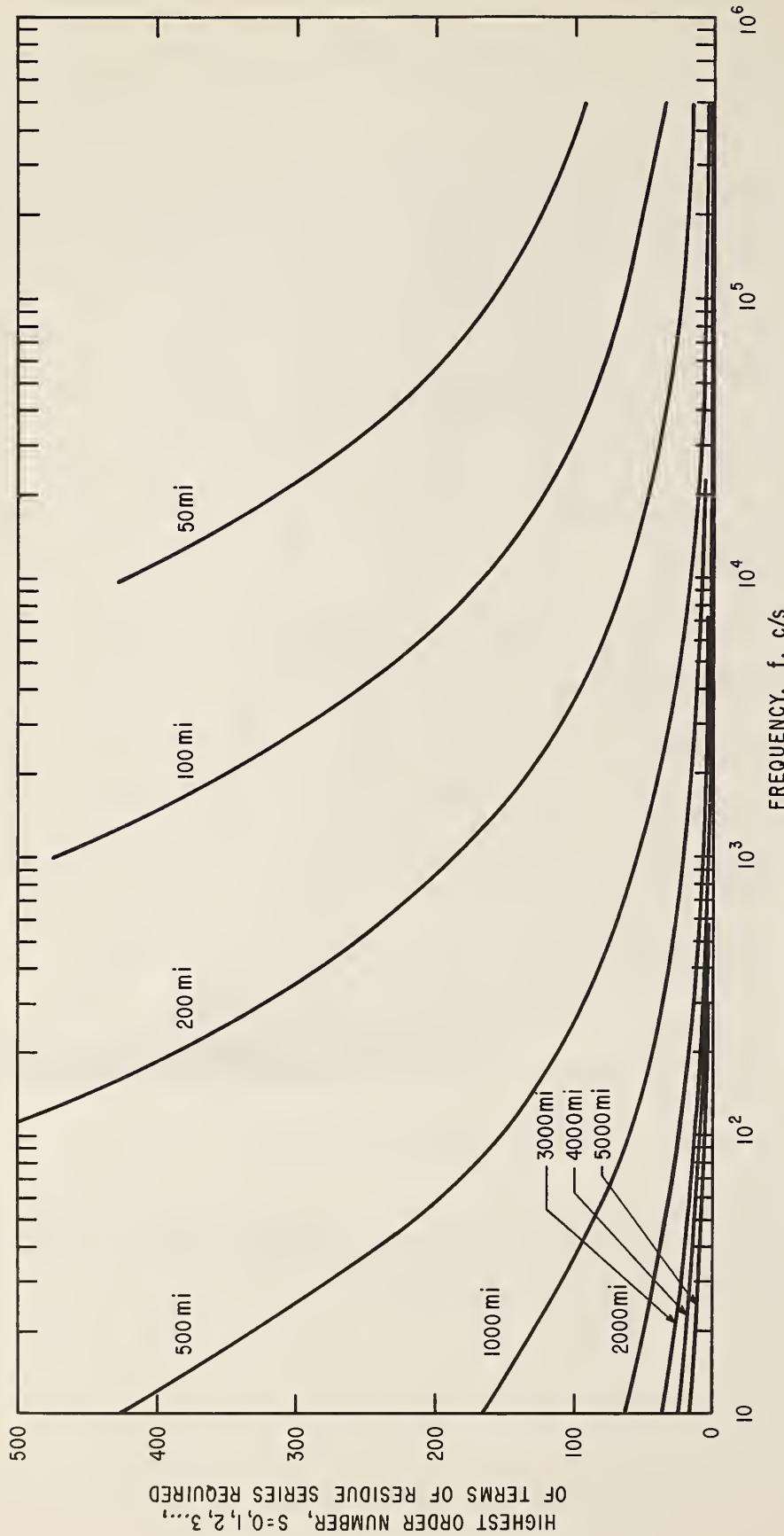


Fig. 2 - Highest order number, $s = 0, 1, 2, 3 \dots$, of terms of the series of residues required for eight significant figure computation precision as a function of frequency for various distances.

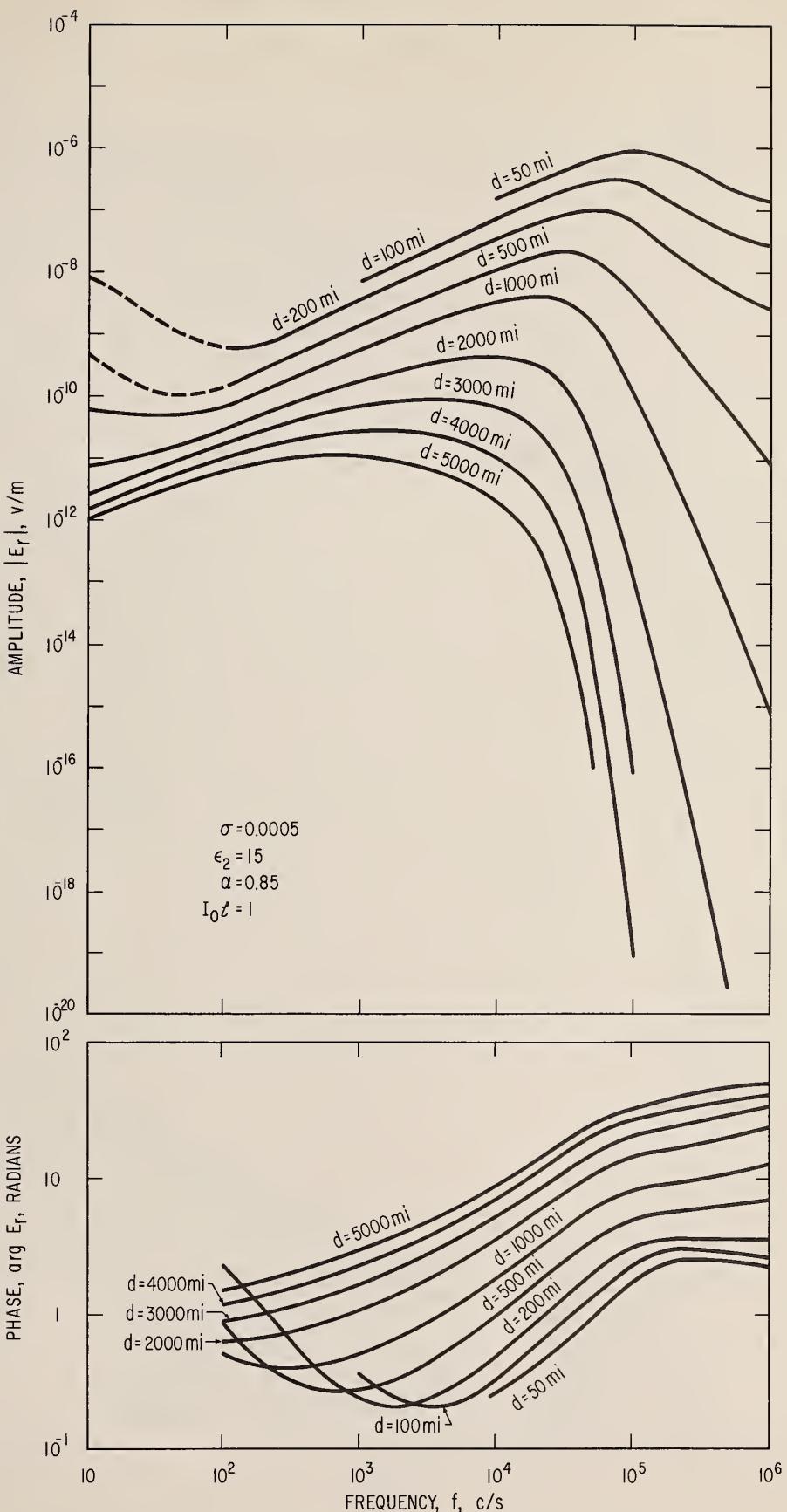


Fig. 3 - Amplitude and phase of the ground wave.

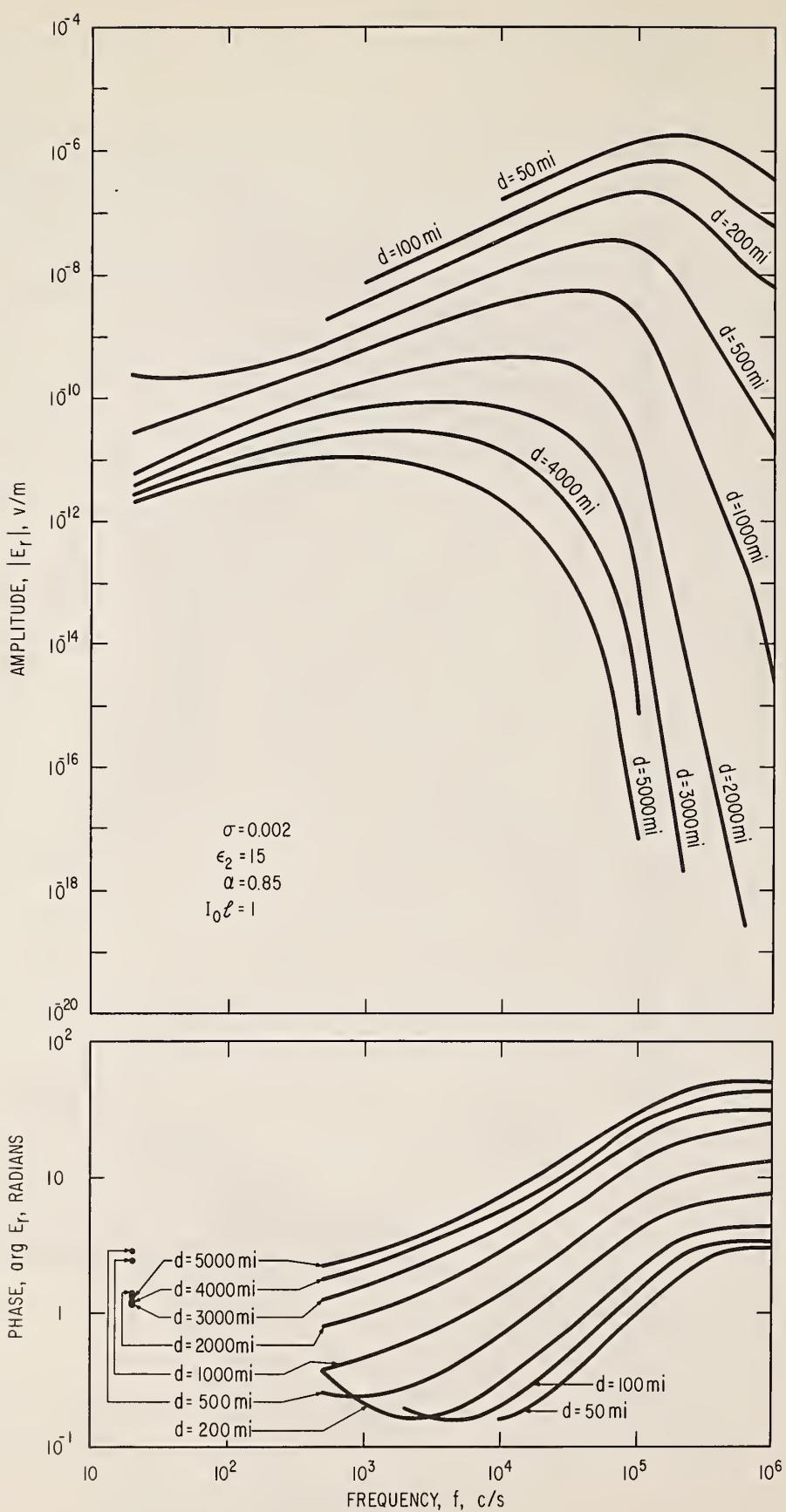


Fig. 4 - Amplitude and phase of the ground wave.

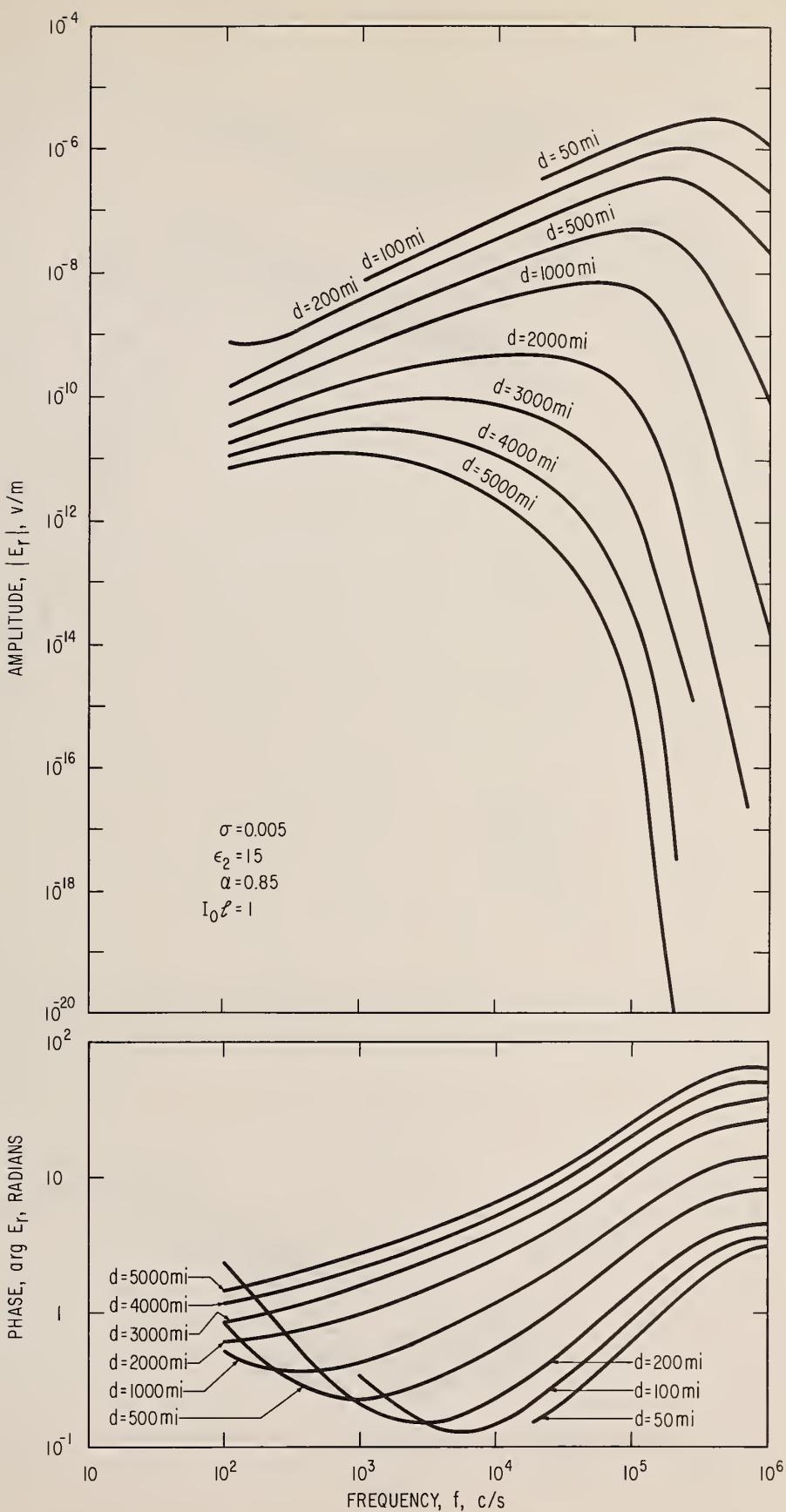


Fig. 5 - Amplitude and phase of the ground wave.

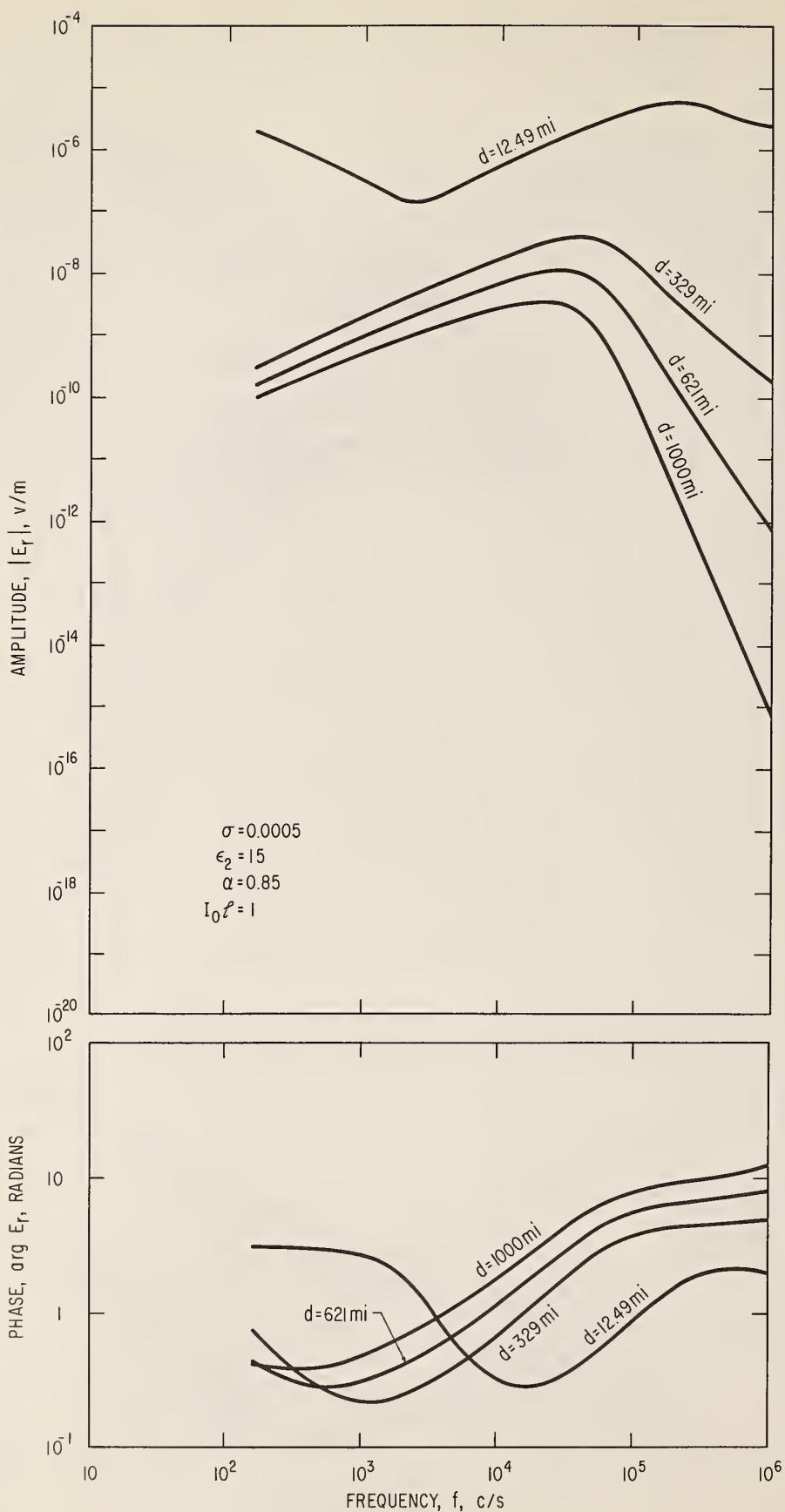


Fig. 6 - Amplitude and phase of the ground wave.

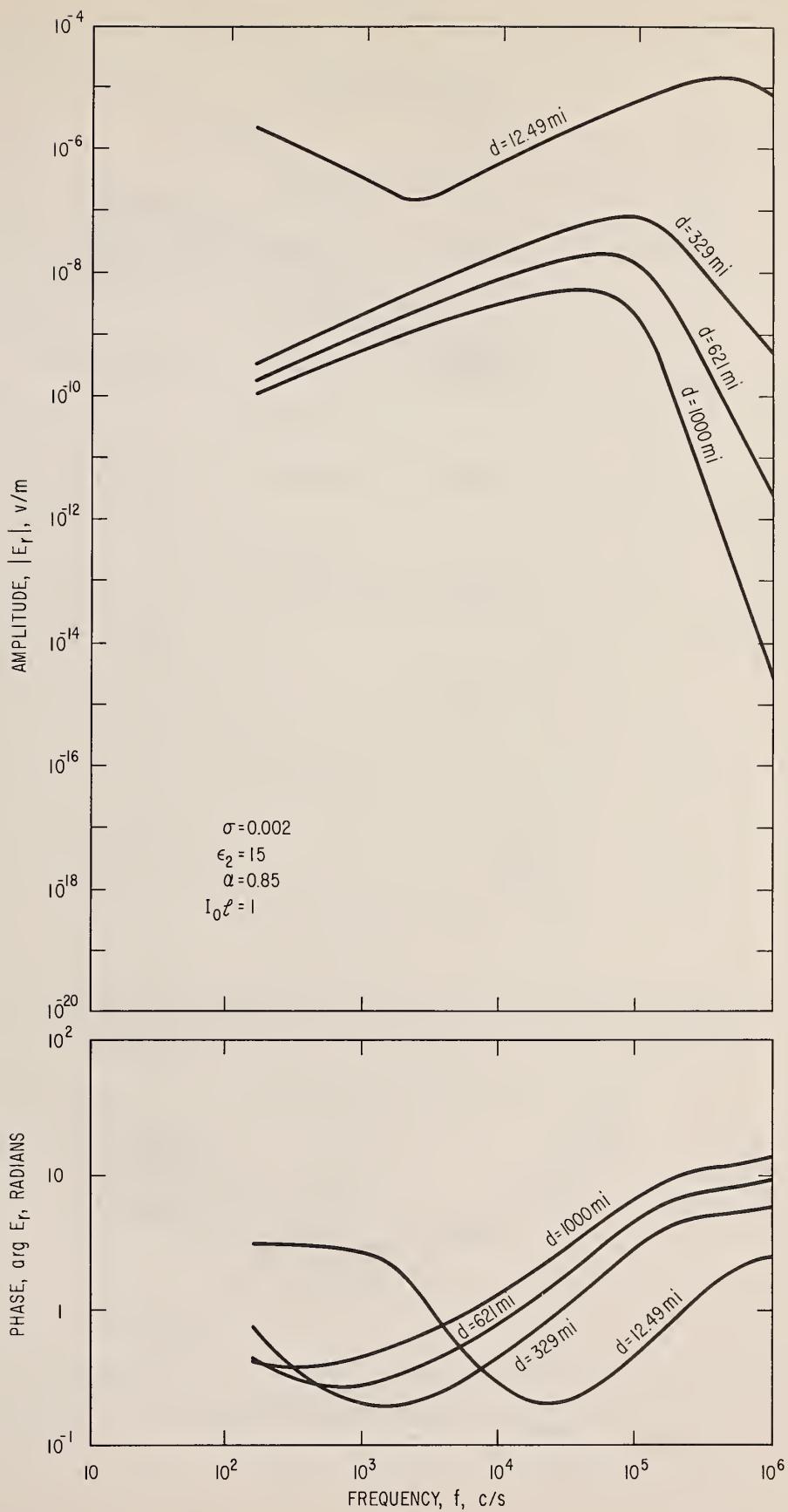


Fig. 7 - Amplitude and phase of the ground wave.

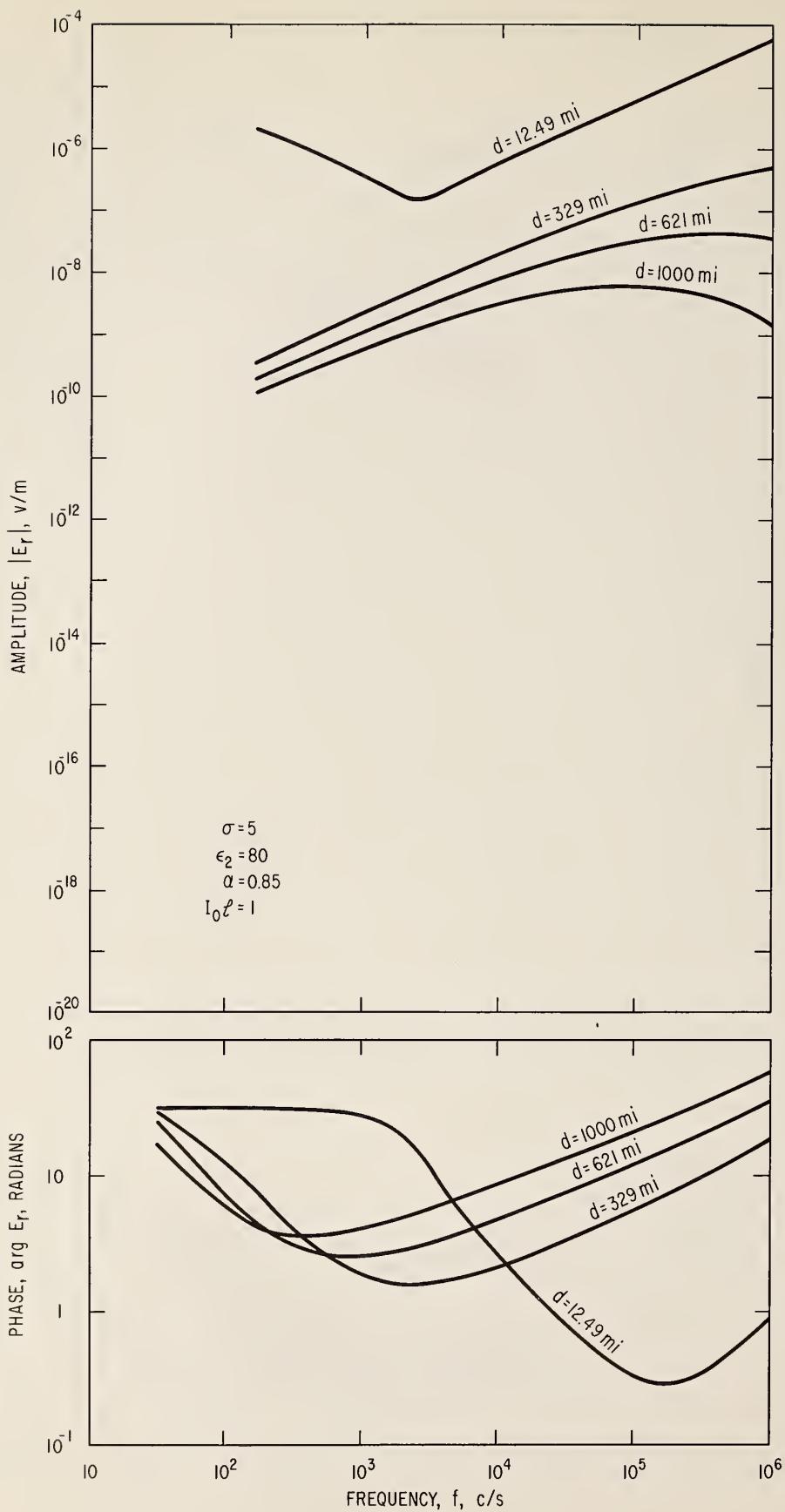


Fig. 8 - Amplitude and phase of the ground wave.

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<u>Table</u>	<u>f, kc</u>	<u>d, mi</u>	<u>σ</u>	<u>ϵ_2</u>	<u>α</u>	<u>Page</u>
1	0.01-1000	5000-500	0.0005	15	0.85	15
2		200-50				16
3	0.02-1000	5000-500	0.002			17
4		200-50				18
5	0.1-1000	5000-500	0.005			19
6		200-50				20
7	0-50 [†]	12.49, 329	0.0005			21
8	50-500 [†]					22
9	500-1000 [†]		0.0005			23
10	0-50 [†]	621, 1000				24
11	50-500 [†]					25
12	500-1000 [†]					26
13	0-50 [†]	12.49, 329	0.002			27
14	50-500 [†]					28
15	500-1000 [†]					29
16	0-50 [†]	621, 1000				30
17	50-500 [†]					31
18	500-1000 [†]					32
19	0-50 [†]	12.49, 329	5	80		33
20	50-500 [†]					34

[†] Tabulated at Gaussian frequencies, f_m .

<u>Table</u>	<u>f, kc</u>	<u>d, mi</u>	<u>σ</u>	<u>ϵ_2</u>	<u>α</u>	<u>Page</u>
21	500-1000 [†]					35
22	0-50 [†]	621, 1000				36
23	50-500 [†]					37
24	500-1000 [†]					38
25	153.5	50-600	0.001-0.006		0.75	39
26	153.5	50-600	0.007-5	15, 80	0.75, 0.85	40

[†]

Tabulated at Gaussian frequencies, f_m .

Table 1

$$\sigma = 0.0005 \quad \epsilon_2 = 15 \quad \alpha = 0.85$$

d = 5000 miles

d = 4000 miles

f, kc	E _r	arg E _r	E _r	arg E _r
0.01	1.0990	-12	1.8208	
0.1	6.6410	-12	1.4586	
0.2	9.2012	-12	1.7232	
0.5	1.1632	-11	2.2608	
1	1.1546	-11	2.8648	
2	9.4242	-12	3.7484	
5	4.9181	-12	5.7289	
10	1.9175	-12	2.1848	
20	2.8707	-13	7.8935	-1
50	1.0117	-16	5.8818	
100	1.05	-22	1.41	
200	3.74	-29	2.36	-1
500	1.966	-38	2.904	
1000				
			3.4618	-39
				1.6389

d = 3000 miles

d = 2000 miles

0.01	2.4916	-12	2.1500	
0.1	1.7081	-11	8.6196	-1
0.2	2.8589	-11	9.7844	-1
0.5	5.0416	-11	1.2768	
1	6.9359	-11	1.6375	
2	8.4659	-11	2.1773	
5	8.7117	-11	3.3985	
10	6.7498	-11	5.0926	
20	2.9086	-11	1.8355	
50	3.4185	-13	2.6409	
100	8.68	-17	1.51	
200	9.87	-21	4.66	
500	2.369	-26	3.631	
1000	1.9596	-31	3.1178	
			1.1865	-23
				4.5968

d = 1000 miles

d = 500 miles

0.01	6.4543	-11	2.9167	
0.1	6.8851	-11	5.1809	-1
0.2	1.3706	-10	3.9547	-1
0.5	3.2211	-10	3.9541	-1
1	5.9590	-10	4.8016	-1
2	1.0671	-9	6.4934	-1
5	2.1436	-9	1.0870	
10	3.2960	-9	1.7262	
20	4.0898	-9	2.8858	
50	1.6033	-9	5.686	
100	9.97	-11	1.62	
200	3.62	-12	2.79	
500	3.960	-14	4.359	
1000	8.3616	-16	6.0759	
			8.3670	-12
				5.3148
				-1

Table 2

$$\sigma = 0.0005 \quad \epsilon_2 = 15 \quad \alpha = 0.85$$

d = 200 miles

d = 100 miles

f, kc	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$
0.01	8.5397	- 9	3.0982	
0.1	7.3828	-10	2.2830	
0.2	6.7000	-10	1.0639	
0.5	1.8400	- 9	3.7040	- 1
1	3.7680	- 9	2.3100	- 1
2	7.5175	- 9	1.9968	- 1
5	1.8403	- 8	2.7898	- 1
10	3.5560	- 8	4.6014	- 1
20	6.5480	- 8	8.2889	- 1
50	1.0791	- 7	1.8435	
100	6.86	- 8	3.00	
200	2.03	- 8	3.51	
500	5.706	- 9	3.509	
1000	2.6896	- 9	3.5519	

d = 50 miles

10	1.5356	- 7	2.4640	- 1
20	3.0137	- 7	3.9173	- 1
50	6.7009	- 7	8.8005	- 1
100	9.12	- 7	1.61	
200	6.03	- 7	2.44	
500	2.164	- 7	2.494	
1000	1.480	- 7	2.252	

Table 3

$$\sigma = 0.002 \quad \epsilon_2 = 15 \quad \alpha = 0.85$$

d = 5000 miles

d = 4000 miles

f, kc	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$
0.02	2.1044	-12	1.3379	2.8146
0.1	6.6346	-12	1.4488	1.0398
0.2	9.1788	-12	1.7026	1.5850
0.5	1.1542	-11	2.2050	2.3607
1	1.1347	-11	2.7452	2.7385
2	9.0964	-12	3.4898	2.6955
5	4.6117	-12	5.0078	1.9342
10	1.9103	-12	6.2694	-1
20	4.9695	-13	3.8241	4.4562
50	1.4156	-14	5.8833	3.1513
100	7.91	-18	4.73	8.97
200	2.86	-25	3.84	1.03
500	1.06	-36	6.37	6.54
1000	6.78	-47	4.71	2.13
				-38
				4.26

d = 3000 miles

d = 2000 miles

0.02	3.9322	-12	1.1543	6.1780	-12	1.3967	
0.1	1.7075	-11	8.5485	-1	3.0629	-11	6.1203
0.2	2.8560	-11	9.6386	-1	5.5838	-11	6.3119
0.5	5.0241	-11	1.2386		1.1476	-10	7.7610
1	6.8794	-11	1.5573		1.8458	-10	9.7402
2	8.3212	-11	2.0071		2.7415	-10	1.2696
5	8.4539	-11	2.9334		3.9494	-10	1.8968
10	6.8394	-11	4.0996		4.4680	-10	2.6945
20	4.1642	-11	6.0631		4.1622	-10	4.0412
50	7.3108	-12	4.9082		1.8141	-10	1.2791
100	1.06	-13	5.67		1.34	-11	6.14
200	3.88	-18	4.36	-1	1.56	-14	5.02
500	4.19	-25	6.22		2.88	-19	2.72
1000	9.33	-31	5.24		4.37	-23	6.22

d = 1000 miles

d = 500 miles

0.02	2.9168	-11	2.4068	2.5786	-10	2.8466	
0.1	6.8848	-11	5.1420	-1	1.3314	-10	8.2959
0.2	1.3704	-10	3.8765	-1	2.8699	-10	4.1737
0.5	3.2199	-10	3.7563	-1	7.2439	-10	2.5557
1	5.9541	-10	4.4014	-1	1.4156	-9	2.3678
2	1.0657	-9	5.6801	-1	2.7236	-9	2.7361
5	2.1474	-9	8.7765	-1	6.2927	-9	4.1580
10	3.3900	-9	1.2971		1.1496	-8	6.3588
20	4.8356	-9	2.0220		2.0013	-8	1.0378
50	5.2378	-9	3.9340		3.3925	-8	2.1323
100	1.97	-9	3.22	-1	2.88	-8	3.71
200	7.30	-11	3.32		5.92	-9	5.63
500	2.30	-13	5.51		2.44	-10	6.24
1000	2.38	-15	9.15	-1	2.09	-11	1.40

Table 4

$$\dot{\sigma} = 0.002 \quad \epsilon_2 = 15 \quad \alpha = 0.85$$

d = 200 miles

d = 100 miles

f, kc	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$
0.5	1.8401	- 9	3.6179	- 1
0.2	6.6998	-10	1.0605	
1	3.7683	- 9	2.1376	- 1
2	7.5206	- 9	1.6515	- 1
5	1.8458	- 8	1.9247	- 1
10	3.6019	- 8	2.8710	- 1
20	6.9075	- 8	4.8588	- 1
50	1.5000	- 7	1.0646	
100	2.10	- 7	1.95	
200	1.33	- 7	3.30	
500	2.14	- 8	4.16	
1000	6.23	- 9	4.28	

d = 50 miles

10	1.5421	- 7	1.6054	- 1
20	3.0655	- 7	2.2083	- 1
50	7.4244	- 7	4.6801	- 1
100	1.35	- 6	8.90	- 1
200	1.89	- 6	1.68	
500	8.90	- 7	2.88	
1000	3.41	- 7	2.91	

Table 5

$$\sigma = 0.005 \quad \epsilon_2 = 15 \quad \alpha = 0.85$$

d = 5000 miles

d = 4000 miles

f, kc	[E _r]	arg E _r	[E _r]	arg E _r
0.1	6.6322	-12	1.4452	1.0396
0.2	9.1704	-12	1.6951	1.5839
0.5	1.1507	-11	2.1846	2.3556
1	1.1269	-11	2.7013	2.7244
2	8.9575	-12	3.3947	2.6645
5	4.4371	-12	4.7418	1.8783
10	1.7980	-12	4.5550	-2
20	4.8447	-13	2.5605	4.3881
50	2.9901	-14	2.5585	5.7979
100	3.927	-16	5.516	2.097
200	5.48	-21	1.27	3.09
500	4.02	-34	4.28	9.28
1000	1.54	-44	1.11	-1
			3.91	-37
				5.08
				-1

d = 3000 miles

d = 2000 miles

0.1	1.7072	-11	8.5224	-1	3.0627	-11	6.0995	-1
0.2	2.8549	-11	9.5850	-1	5.5828	-11	6.2698	-1
0.5	5.0172	-11	1.2245		1.1469	-10	7.6529	-1
1	6.8563	-11	1.5278		1.8427	-10	9.5173	-1
2	8.2569	-11	1.9445		2.7304	-10	1.2232	
5	8.2863	-11	2.7619		3.9072	-10	1.7725	
10	6.6318	-11	3.7295		4.3974	-10	2.4301	
20	4.1419	-11	5.2668		4.1816	-10	3.4784	
50	1.1716	-11	2.8280		2.5323	-10	6.1045	
100	1.167	-12	2.205		6.946	-11	3.691	
200	1.82	-15	4.91		1.15	-12	3.59	
500	2.23	-23	2.10		5.74	-18	4.14	
1000	1.03	-29	9.04	-1	2.92	-22	1.30	

d = 1000 miles

d = 500 miles

0.1	6.8847	-11	5.1277	-1	1.3314	-10	8.2858	-1
0.2	1.3704	-10	3.8477	-1	2.8699	-10	4.1536	-1
0.5	3.2194	-10	3.6837	-1	7.2436	-10	2.5052	-1
1	5.9516	-10	4.2544	-1	1.4154	-9	2.2665	-1
2	1.0646	-9	5.3811	-1	2.7232	-9	2.5323	-1
5	2.1423	-9	8.0055	-1	6.2933	-9	3.6426	-1
10	3.3840	-9	1.1379		1.1522	-8	5.3156	-1
20	4.9050	-9	1.6924		2.0309	-8	8.2657	-1
50	6.3679	-9	3.0981		3.8271	-8	1.6079	
100	4.812	-9	5.178		4.795	-8	2.786	
200	8.41	-10	2.27		2.73	-8	4.75	
500	1.72	-12	6.19		1.11	-9	9.33	-1
1000	9.63	-15	1.70		6.58	-11	1.89	

Table 6

$\sigma = 0.005$ $\epsilon_2 = 15$ $\alpha = 0.85$

$d = 200$ miles

$d = 100$ miles

f, kc	$[E_r]$	$\arg E_r$	$[E_r]$	$\arg E_r$
0.1	7.3828	-10	2.2806	
0.2	6.6998	-10	1.0592	
0.5	1.8401	-9	3.5863	-1
1	3.7683	-9	2.0742	-1
2	7.5209	-9	1.5246	-1
5	1.8466	-8	1.6065	-1
10	3.6091	-8	2.2328	-1
20	6.9687	-8	3.5800	-1
50	1.5921	-7	7.4895	-1
100	2.670	-7	1.367	
200	3.14	-7	2.47	
500	7.66	-8	4.19	
1000	1.69	-8	4.60	

$d = 50$ miles

20	3.0742	- 7	1.5765	- 1
50	7.5600	- 7	3.1110	- 1
100	1.451	- 6	5.846	- 1
200	2.53	- 6	1.12	
500	2.67	- 6	2.44	

Table 7

 $\sigma = 0.0005$ $\epsilon_2 = 15$ $\alpha = 0.85$

d = 12.49 miles

d = 329 miles

\dagger f, kc	E _r	arg E _r	E _r	arg E _r
0.030725	1.1456	- 5	3.1289	1.0573
0.16175	2.1713	- 6	3.0746	3.3338
0.39689	8.7482	- 7	2.9746	8.8931
0.73521	4.5755	- 7	2.8177	1.6570
1.1753	2.7036	- 7	2.5709	2.6295
1.7153	1.7778	- 7	2.1692	3.7981
2.3530	1.4836	- 7	1.6078	5.1511
3.0857	1.6796	- 7	1.1089	6.6750
3.9103	2.1409	- 7	7.9887	- 1
4.8233	2.7237	- 7	6.1712	- 1
5.8210	3.3756	- 7	5.0469	- 1
6.8991	4.0786	- 7	4.3115	- 1
8.0532	4.8254	- 7	3.8124	- 1
9.2783	5.6119	- 7	3.4673	- 1
10.569	6.4348	- 7	3.2286	- 1
11.921	7.2911	- 7	3.0665	- 1
13.327	8.1773	- 7	2.9617	- 1
14.783	9.0898	- 7	2.9009	- 1
16.281	1.0025	- 6	2.8744	- 1
17.816	1.0979	- 6	2.8751	- 1
19.381	1.1947	- 6	2.8978	- 1
20.969	1.2925	- 6	2.9381	- 1
22.575	1.3910	- 6	2.9926	- 1
24.190	1.4896	- 6	3.0587	- 1
25.810	1.5880	- 6	3.1339	- 1
27.425	1.6856	- 6	3.2163	- 1
29.031	1.7822	- 6	3.3041	- 1
30.619	1.8772	- 6	3.3960	- 1
32.184	1.9703	- 6	3.4905	- 1
33.719	2.0611	- 6	3.5865	- 1
35.217	2.1492	- 6	3.6829	- 1
36.673	2.2343	- 6	3.7788	- 1
38.079	2.3161	- 6	3.8732	- 1
39.431	2.3942	- 6	3.9655	- 1
40.722	2.4684	- 6	4.0548	- 1
41.947	2.5385	- 6	4.1405	- 1
43.101	2.6041	- 6	4.2220	- 1
44.179	2.6650	- 6	4.2987	- 1
45.177	2.7211	- 6	4.3703	- 1
46.090	2.7723	- 6	4.4361	- 1
46.914	2.8182	- 6	4.4958	- 1
47.647	2.8589	- 6	4.5490	- 1
48.285	2.8942	- 6	4.5955	- 1
48.825	2.9240	- 6	4.6350	- 1
49.265	2.9482	- 6	4.6673	- 1
49.603	2.9668	- 6	4.6921	- 1
49.838	2.9797	- 6	4.7094	- 1
49.969	2.9868	- 6	4.7190	- 1

 \dagger Gaussian frequencies, interval: 0-50 kc.

Table 8

$\sigma = 0.0005$ $\epsilon_2 = 15$ $\alpha = 0.85$

† f, kc	d = 12.49 miles			d = 329 miles		
	E _r	arg E _r	E _r	arg E _r		
50.277	3.0036	- 6	4.7416	- 1	4.42	- 8
51.456	3.0679	- 6	4.8286	- 1	4.37	- 8
53.572	3.1820	- 6	4.9855	- 1	4.29	- 8
56.617	3.3438	- 6	5.2128	- 1	4.14	- 8
60.578	3.5497	- 6	5.5103	- 1	3.93	- 8
65.438	3.7949	- 6	5.8772	- 1	3.03	- 8
71.177	4.0735	- 6	6.3113	- 1	2.82	- 8
77.771	4.3780	- 6	6.8092	- 1	2.51	- 8
85.193	4.7001	- 6	7.3665	- 1	2.16	- 8
93.410	5.0302	- 6	7.9771	- 1	1.82	- 8
102.39	5.3581	- 6	8.6344	- 1	1.51	- 8
112.09	5.6734	- 6	9.3303	- 1	1.25	- 8
122.48	5.9659	- 6	1.0056		1.13	- 8
133.50	6.2264	- 6	1.0803		9.33	- 9
145.12	6.4472	- 6	1.1562		7.75	- 9
157.29	6.6224	- 6	1.2322		6.52	- 9
169.95	6.7485	- 6	1.3074		5.53	- 9
183.05	6.8246	- 6	1.3810		4.75	- 9
196.53	6.8519	- 6	1.4521		4.11	- 9
210.34	6.8338	- 6	1.5200		3.59	- 9
224.43	6.7754	- 6	1.5841		3.16	- 9
238.72	6.6828	- 6	1.6440		2.81	- 9
253.17	6.5628	- 6	1.6992		2.51	- 9
267.71	6.4222	- 6	1.7496		2.25	- 9
282.29	6.2674	- 6	1.7951		2.04	- 9
296.83	6.1043	- 6	1.8358		1.86	- 9
311.28	5.9378	- 6	1.8719		1.698	- 9
325.57	5.7721	- 6	1.9035		1.563	- 9
339.66	5.6105	- 6	1.9309		1.4453	- 9
353.47	5.4552	- 6	1.9546		1.3433	- 9
366.95	5.3081	- 6	1.9748		1.2545	- 9
380.05	5.1702	- 6	1.9919		1.1769	- 9
392.71	5.0422	- 6	2.0063		1.1089	- 9
404.88	4.9243	- 6	2.0183		1.0494	- 9
416.50	4.8165	- 6	2.0282		9.9725	- 10
427.52	4.7186	- 6	2.0363		9.5148	- 10
437.91	4.6303	- 6	2.0430		9.1138	- 10
447.61	4.5512	- 6	2.0483		8.7632	- 10
456.59	4.4809	- 6	2.0526		8.4577	- 10
464.81	4.4188	- 6	2.0560		8.1929	- 10
472.23	4.3646	- 6	2.0586		7.9650	- 10
478.82	4.3181	- 6	2.0607		7.7709	- 10
484.56	4.2786	- 6	2.0623		7.6081	- 10
489.42	4.2459	- 6	2.0634		7.4745	- 10
493.38	4.2198	- 6	2.0643		7.3684	- 10
496.43	4.2001	- 6	2.0649		7.2885	- 10
498.54	4.1865	- 6	2.0653		7.2337	- 10
499.72	4.1791	- 6	2.0655		7.2035	- 10

† Gaussian frequencies, interval: 50-500 kc.

Table 9

 $\sigma = 0.0005 \quad \epsilon_2 = 15 \quad \alpha = 0.85$

\dagger f, kc	$d = 12.49 \text{ miles}$		$d = 329 \text{ miles}$	
	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$
500.31	4.1754	- 6	2.0656	7.1886 -10
501.62	4.1671	- 6	2.0658	7.1554 -10
503.97	4.1524	- 6	2.0662	7.0964 -10
507.35	4.1315	- 6	2.0667	7.0128 -10
511.75	4.1048	- 6	2.0673	6.9064 -10
517.15	4.0728	- 6	2.0678	6.7794 -10
523.53	4.0359	- 6	2.0683	6.6342 -10
530.86	3.9949	- 6	2.0687	6.4734 -10
539.10	3.9503	- 6	2.0688	6.2998 -10
548.23	3.9031	- 6	2.0688	6.1162 -10
558.21	3.8532	- 6	2.0684	5.9251 -10
568.99	3.8024	- 6	2.0676	5.7291 -10
580.53	3.7500	- 6	2.0664	5.5305 -10
592.78	3.6975	- 6	2.0648	5.3315 -10
605.69	3.6452	- 6	2.0627	5.1338 -10
619.21	3.5931	- 6	2.0604	4.9390 -10
633.27	3.5429	- 6	2.0575	4.7485 -10
647.83	3.4939	- 6	2.0542	4.5634 -10
662.81	3.4461	- 6	2.0506	4.3844 -10
678.16	3.3998	- 6	2.0469	4.2123 -10
693.81	3.3560	- 6	2.0427	4.0474 -10
709.69	3.3154	- 6	2.0388	3.8902 -10
725.75	3.2775	- 6	2.0335	3.7408 -10
741.90	3.2375	- 6	2.0288	3.5993 -10
758.10	3.2004	- 6	2.0250	3.4657 -10
774.25	3.1745	- 6	2.0221	3.3399 -10
790.31	3.1330	- 6	2.0130	3.2217 -10
806.19	3.0999	- 6	2.0087	3.1109 -10
821.84	3.0836	- 6	2.0076	3.0074 -10
837.19	3.0538	- 6	2.0000	2.9110 -10
852.17	3.0371	- 6	1.9978	2.8213 -10
866.73	3.0135	- 6	1.9949	2.7381 -10
880.79	3.0557	- 6	1.9833	2.6612 -10
894.31	2.9261	- 6	1.9763	2.5904 -10
907.22	2.9456	- 6	2.0036	2.5253 -10
919.47	2.9758	- 6	1.9502	2.4658 -10
931.01	2.9678	- 6	1.9663	2.4117 -10
941.79	2.8875	- 6	1.9611	2.3627 -10
951.77	2.8976	- 6	1.9967	2.3187 -10
960.90	2.8472	- 6	1.9869	2.2794 -10
969.14	2.9055	- 6	1.9746	2.2449 -10
976.47	2.8803	- 6	1.9512	2.2148 -10
982.85	2.8839	- 6	1.9691	2.1891 -10
988.25	2.7757	- 6	1.9851	2.1677 -10
992.65	2.8165	- 6	1.9074	2.1504 -10
996.03	2.8653	- 6	1.9649	2.1373 -10
998.38	2.9340	- 6	1.9228	2.1283 -10
999.69	2.8464	- 6	1.9773	2.1233 -10

\dagger Gaussian frequencies, interval: 500-1000 kc.

Table 10

$$\sigma = 0.0005 \quad \epsilon_2 = 15 \quad \alpha = 0.85$$

\dagger f, kc	d = 621 miles			d = 1000 miles		
	$ E_r $	arg E_r	$ E_r $	arg E_r		
0.030725	7.9832	-11	2.4046	2.2340	-11	1.6720
0.16175	1.8504	-10	4.4409	1.1158	-10	4.1786
0.39689	4.5575	-10	2.9672	2.6084	-10	3.8290
0.73521	8.2308	-10	2.9082	4.5513	-10	4.3354
1.1753	1.2781	-9	3.2295	6.8479	-10	5.1098
1.7153	1.8107	-9	3.7273	9.4105	-10	6.0287
2.3530	2.4106	-9	4.3369	1.2162	-9	7.0530
3.0857	3.0676	-9	5.0317	1.5035	-9	8.1662
3.9103	3.7715	-9	5.7983	1.7967	-9	9.3602
4.8233	4.5117	-9	6.6288	2.0902	-9	1.0630
5.8210	5.2778	-9	7.5174	2.3788	-9	1.1970
6.8991	6.0589	-9	8.4594	2.6576	-9	1.3378
8.0532	6.8439	-9	9.4505	2.9219	-9	1.4848
9.2783	7.6218	-9	1.0486	3.1673	-9	1.6375
10.569	8.3814	-9	1.1563	3.3898	-9	1.7955
11.921	9.1116	-9	1.2674	3.5857	-9	1.9582
13.327	9.8022	-9	1.3817	3.7520	-9	2.1248
14.783	1.0443	-8	1.4986	3.8864	-9	2.2948
16.281	1.1026	-8	1.6175	3.9873	-9	2.4673
17.816	1.1544	-8	1.7379	4.0538	-9	2.6417
19.381	1.1990	-8	1.8592	4.0862	-9	2.8171
20.969	1.2361	-8	1.9809	4.0855	-9	2.9926
22.575	1.2655	-8	2.1024	4.0537	-9	3.1676
24.190	1.287	-8	2.2223	3.993	-9	3.341
25.810	1.301	-8	2.342	3.908	-9	3.512
27.425	1.308	-8	2.460	3.801	-9	3.680
29.031	1.308	-8	2.575	3.677	-9	3.845
30.619	1.302	-8	2.687	3.539	-9	4.004
32.184	1.291	-8	2.796	3.392	-9	4.159
33.719	1.275	-8	2.901	3.240	-9	4.308
35.217	1.26	-8	3.00	3.09	-9	4.45
36.673	1.23	-8	3.10	2.93	-9	4.59
38.079	1.21	-8	3.19	2.78	-9	4.71
39.431	1.18	-8	3.28	2.64	-9	4.84
40.722	1.15	-8	3.36	2.50	-9	4.95
41.947	1.13	-8	3.43	2.37	-9	5.05
43.101	1.10	-8	3.50	2.25	-9	5.15
44.179	1.07	-8	3.57	2.14	-9	5.24
45.177	1.05	-8	3.62	2.04	-9	5.32
46.090	1.03	-8	3.68	1.96	-9	5.39
46.914	1.01	-8	3.72	1.88	-9	5.46
47.647	9.88	-9	3.76	1.81	-9	5.51
48.285	9.71	-9	3.80	1.75	-9	5.56
48.825	9.57	-9	3.83	1.70	-9	5.60
49.265	9.46	-9	3.85	1.67	-9	5.63
49.603	9.37	-9	3.87	1.64	-9	5.66
49.838	9.31	-9	3.88	1.62	-9	5.67
49.969	9.28	-9	3.89	1.61	-9	5.68

\dagger Gaussian frequencies, interval: 0-50kc.

Table 11

 $\sigma = 0.0005$ $\epsilon_2 = 15$ $\alpha \approx 0.85$

† f, kc	d = 621 miles			d = 1000 miles		
	E _r	arg E _r	E _r	arg E _r	arg E _r	arg E _r
50.277	9.20	- 9	3.91	1.58	- 9	5.71
51.456	8.89	- 9	3.97	1.48	- 9	5.79
53.572	8.34	- 9	4.07	1.32	- 9	5.93
56.617	7.58	- 9	4.22	1.11	- 9	6.12
60.578	6.63	- 9	4.39	8.83	-10	5.78
65.438	4.52	- 9	4.35	4.64	-10	6.28
71.177	4.09	- 9	4.71	4.07	-10	5.00
77.771	3.38	- 9	5.00	3.05	-10	8.88
85.193	2.64	- 9	5.23	2.10	-10	1.20
				1.38	-10	1.46
102.39	1.50	- 9	5.58	8.92	-11	1.67
112.09	1.12	- 9	5.72	5.77	-11	1.86
122.48	8.31	-10	5.85	3.75	-11	2.02
133.50	6.27	-10	5.95	2.48	-11	2.17
145.12	4.79	-10	6.04	1.66	-11	2.30
157.29	3.70	-10	6.12	1.13	-11	2.43
169.95	2.89	-10	6.20	7.84	-12	2.55
183.05	2.29	-10	6.26	5.51	-12	2.66
196.53	1.83	-10	4.48	- 2	3.93	-12
210.34	1.48	-10	1.05	- 1	2.84	-12
224.43	1.20	-10	1.62	- 1	2.09	-12
238.72	9.92	-11	2.16	- 1	1.55	-12
253.17	8.24	-11	2.68	- 1	1.17	-12
267.71	6.92	-11	3.17	- 1	8.96	-13
282.29	5.85	-11	3.65	- 1	6.93	-13
296.83	4.99	-11	4.10	- 1	5.43	-13
311.28	4.298	-11	4.529	- 1	4.307	-13
325.57	3.729	-11	4.941	- 1	3.456	-13
339.66	3.2601	-11	5.3352	- 1	2.8048	-13
353.47	2.8721	-11	5.7106	- 1	2.3025	-13
366.95	2.5493	-11	6.0679	- 1	1.9113	-13
380.05	2.2793	-11	6.4069	- 1	1.6042	-13
392.71	2.0525	-11	6.7278	- 1	1.3611	-13
404.88	1.8613	-11	7.0304	- 1	1.1672	-13
416.50	1.6996	-11	7.3145	- 1	1.0116	-13
427.52	1.5626	-11	7.5801	- 1	8.8597	-14
437.91	1.4462	-11	7.8268	- 1	7.8402	-14
447.61	1.3474	-11	8.0545	- 1	7.0096	-14
456.59	1.2636	-11	8.2630	- 1	6.3312	-14
464.81	1.1926	-11	8.4519	- 1	5.7767	-14
472.23	1.1329	-11	8.6210	- 1	5.3239	-14
478.82	1.0830	-11	8.7703	- 1	4.9561	-14
484.56	1.0418	-11	8.8993	- 1	4.6598	-14
489.42	1.0085	-11	9.0080	- 1	4.4249	-14
493.38	9.8238	-12	9.0962	- 1	4.2436	-14
496.43	9.6287	-12	9.1638	- 1	4.1101	-14
498.54	9.4960	-12	9.2107	- 1	4.0202	-14
499.72	9.4231	-12	9.2367	- 1	3.9711	-14

† Gaussian frequencies, interval: 50-500 kc.

Table 12

 $\sigma = 0.0005$ $\epsilon_2 = 15$ $\alpha = 0.85$

\dagger f, kc	d = 621 miles			d = 1000 miles		
	$ E_r $	arg E_r	$ E_r $	arg E_r		
500.31	9.3873	-12	9.2496	- 1	3.9470	-14
501.62	9.3075	-12	9.2786	- 1	3.8937	-14
503.97	9.1665	-12	9.3304	- 1	3.8000	-14
507.35	8.9683	-12	9.4047	- 1	3.6697	-14
511.75	8.7186	-12	9.5011	- 1	3.5080	-14
517.15	8.4243	-12	9.6188	- 1	3.3206	-14
523.53	8.0928	-12	9.7571	- 1	3.1142	-14
530.86	7.7322	-12	9.9151	- 1	2.8951	-14
539.10	7.3504	-12	1.0092		2.6696	-14
548.23	6.9553	-12	1.0286		2.4433	-14
558.21	6.5538	-12	1.0497		2.2209	-14
568.99	6.1525	-12	1.0722		2.0064	-14
580.53	5.7568	-12	1.0962		1.8029	-14
592.78	5.3714	-12	1.1215		1.6125	-14
605.69	4.9998	-12	1.1478		1.4364	-14
619.21	4.6450	-12	1.1752		1.2753	-14
633.27	4.3087	-12	1.2034		1.1294	-14
647.83	3.9924	-12	1.2324		9.9821	-15
662.81	3.6967	-12	1.2620		8.8109	-15
678.16	3.4217	-12	1.2920		7.7715	-15
693.81	3.1671	-12	1.3223		6.8537	-15
709.69	2.9325	-12	1.3529		6.0466	-15
725.75	2.7170	-12	1.3835		5.3394	-15
741.90	2.5197	-12	1.4140		4.7214	-15
758.10	2.3396	-12	1.4444		4.1826	-15
774.25	2.1755	-12	1.4745		3.7136	-15
790.31	2.0263	-12	1.5042		3.3060	-15
806.19	1.8910	-12	1.5333		2.9519	-15
821.84	1.7684	-12	1.5618		2.6446	-15
837.19	1.6575	-12	1.5896		2.3781	-15
852.17	1.5575	-12	1.6165		2.1468	-15
866.73	1.4673	-12	1.6425		1.9463	-15
880.79	1.3861	-12	1.6675		1.7724	-15
894.31	1.3133	-12	1.6914		1.6217	-15
907.22	1.2480	-12	1.7140		1.4911	-15
919.47	1.1897	-12	1.7354		1.3781	-15
931.01	1.1378	-12	1.7555		1.2803	-15
941.79	1.0918	-12	1.7742		1.1961	-15
951.77	1.0512	-12	1.7914		1.1236	-15
960.90	1.0157	-12	1.8070		1.0616	-15
969.14	9.8483	-13	1.8212		1.0089	-15
976.47	9.5837	-13	1.8337		9.6450	-16
982.85	9.3604	-13	1.8445		9.2766	-16
988.25	9.1762	-13	1.8537		8.9769	-16
992.65	9.0294	-13	1.8612		8.7408	-16
996.03	8.9184	-13	1.8669		8.5639	-16
998.38	8.8423	-13	1.8709		8.4434	-16
999.69	8.8002	-13	1.8731		8.3771	-16

\dagger Gaussian frequencies, interval: 500-1000 kc.

Table 13

 $\sigma = 0.002$ $\epsilon_2 = 15$ $\alpha = 0.85$

d = 12.49 miles

d = 329 miles

\dagger f, kc	$[E_r]$	$\arg E_r$	$[E_r]$	$\arg E_r$
0.030725	1.1456	- 5	3.01288	5.8965
0.16175	2.01713	- 6	3.0739	3.3338
0.39689	8.7482	- 7	2.9729	8.8931
0.73521	4.5756	- 7	2.8146	1.6570
1.1753	2.07037	- 7	2.5658	2.6297
1.7153	1.07778	- 7	2.1619	3.7992
2.3530	1.04837	- 7	1.5977	5.1546
3.0857	1.6799	- 7	1.0956	6.6838
3.9103	2.01413	- 7	7.8208	- 1
4.8233	2.07246	- 7	5.9642	- 1
5.8210	3.0772	- 7	4.07971	- 1
6.8991	4.0813	- 7	4.0155	- 1
8.0532	4.08298	- 7	3.4669	- 1
9.2783	5.06187	- 7	3.0694	- 1
10.569	6.04451	- 7	2.7753	- 1
11.921	7.03059	- 7	2.5554	- 1
13.327	8.01980	- 7	2.3905	- 1
14.783	9.01181	- 7	2.2674	- 1
16.281	1.0063	- 6	2.01770	- 1
17.816	1.01028	- 6	2.01124	- 1
19.381	1.02011	- 6	2.0684	- 1
20.969	1.03006	- 6	2.0412	- 1
22.575	1.04011	- 6	2.0276	- 1
24.190	1.05020	- 6	2.0252	- 1
25.810	1.06030	- 6	2.0320	- 1
27.425	1.07037	- 6	2.0462	- 1
29.031	1.08036	- 6	2.0665	- 1
30.619	1.09023	- 6	2.0917	- 1
32.184	1.09994	- 6	2.1206	- 1
33.719	2.0945	- 6	2.1524	- 1
35.217	2.01873	- 6	2.1864	- 1
36.673	2.02772	- 6	2.2217	- 1
38.079	2.03641	- 6	2.2579	- 1
39.431	2.04474	- 6	2.2942	- 1
40.722	2.05269	- 6	2.3302	- 1
41.947	2.06023	- 6	2.3655	- 1
43.101	2.06732	- 6	2.3997	- 1
44.179	2.07393	- 6	2.4323	- 1
45.177	2.08005	- 6	2.4630	- 1
46.090	2.08564	- 6	2.4916	- 1
46.914	2.09069	- 6	2.5177	- 1
47.647	2.09517	- 6	2.5413	- 1
48.285	2.09907	- 6	2.5619	- 1
48.825	3.00237	- 6	2.5795	- 1
49.265	3.00505	- 6	2.5940	- 1
49.603	3.00712	- 6	2.6051	- 1
49.838	3.00855	- 6	2.6129	- 1
49.969	3.00935	- 6	2.6172	- 1
			7.02632	- 8

 \dagger Gaussian frequencies, interval: 0-50 kc.

Table 14

$\sigma = 0.002$ $\epsilon_2 = 15$ $\alpha = 0.85$

$d = 12.49$ miles

$d = 329$ miles

\dagger f, kc	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$
50.277	3.1122	- 6	2.6275	- 1
51.456	3.1841	- 6	2.6670	- 1
53.572	3.3127	- 6	2.7391	- 1
56.617	3.4973	- 6	2.8451	- 1
60.578	3.7364	- 6	2.9866	- 1
65.438	4.0281	- 6	3.1645	- 1
71.177	4.3699	- 6	3.3795	- 1
77.771	4.7590	- 6	3.6313	- 1
85.193	5.1919	- 6	3.9194	- 1
93.410	5.6643	- 6	4.2424	- 1
102.39	6.1717	- 6	4.5988	- 1
112.09	6.7088	- 6	4.9865	- 1
122.48	7.2697	- 6	5.4032	- 1
133.50	7.8483	- 6	5.8463	- 1
145.12	8.4380	- 6	6.3132	- 1
157.29	9.0319	- 6	6.8011	- 1
169.95	9.6231	- 6	7.3068	- 1
183.05	1.0205	- 5	7.8274	- 1
196.53	1.0770	- 5	8.3598	- 1
210.34	1.1313	- 5	8.9007	- 1
224.43	1.1828	- 5	9.4470	- 1
238.72	1.2310	- 5	9.9956	- 1
253.17	1.2755	- 5	1.0543	1.68
267.71	1.3160	- 5	1.1087	1.44
282.29	1.3522	- 5	1.1625	1.25
296.83	1.3841	- 5	1.2153	1.09
311.28	1.4116	- 5	1.2669	9.60
325.57	1.4349	- 5	1.3171	8.53
339.66	1.4539	- 5	1.3657	7.64
353.47	1.4691	- 5	1.4124	6.89
366.95	1.4806	- 5	1.4572	6.26
380.05	1.4888	- 5	1.4998	5.72
392.71	1.4941	- 5	1.5402	5.26
404.88	1.4968	- 5	1.5782	4.87
416.50	1.4973	- 5	1.6139	4.53
427.52	1.4960	- 5	1.6470	4.25
437.91	1.4934	- 5	1.6776	4.00
447.61	1.4896	- 5	1.7057	3.78
456.59	1.4851	- 5	1.7312	3.60
464.81	1.4802	- 5	1.7541	3.44
472.23	1.4751	- 5	1.7745	3.31
478.82	1.4701	- 5	1.7924	3.20
484.56	1.4654	- 5	1.8077	3.10
489.42	1.4612	- 5	1.8206	3.03
493.38	1.4576	- 5	1.8309	2.97
496.43	1.4547	- 5	1.8389	2.92
498.54	1.4527	- 5	1.8443	2.89
499.72	1.4515	- 5	1.8474	2.87

\dagger Gaussian frequencies, interval: 50-500 kc.

Table 15

$$\sigma = 0.002 \quad \epsilon_2 = 15 \quad \alpha = 0.85$$

d = 12.49 miles

d = 329 miles

\dagger f, kc	[E _r]	arg E _r	[E _r]	arg E _r
500.31	1.4509	- 5	1.8489	5.26
501.62	1.4496	- 5	1.8522	5.26
503.97	1.4472	- 5	1.8582	5.27
507.35	1.4437	- 5	1.8668	5.27
511.75	1.4390	- 5	1.8779	5.28
517.15	1.4331	- 5	1.8913	5.28
523.53	1.4257	- 5	1.9069	5.29
530.86	1.4170	- 5	1.9246	5.30
539.10	1.4066	- 5	1.9441	5.31
548.23	1.3947	- 5	1.9652	5.32
558.21	1.3812	- 5	1.9878	5.33
568.99	1.3660	- 5	2.0115	5.34
580.53	1.3491	- 5	2.0361	5.36
592.78	1.3307	- 5	2.0614	5.37
605.69	1.3107	- 5	2.0871	5.38
619.21	1.2893	- 5	2.1129	5.40
633.27	1.2667	- 5	2.1387	5.413
647.83	1.2430	- 5	2.1642	5.428
662.81	1.2183	- 5	2.1892	5.442
678.16	1.1930	- 5	2.2135	5.457
693.81	1.1673	- 5	2.2370	5.472
709.69	1.1412	- 5	2.2595	5.486
725.75	1.1152	- 5	2.2808	5.5006
741.90	1.0893	- 5	2.3010	5.5148
758.10	1.0637	- 5	2.3199	5.5288
774.25	1.0388	- 5	2.3374	5.5424
790.31	1.0145	- 5	2.3537	5.5558
806.19	9.9101	- 6	2.3686	5.5687
821.84	9.6849	- 6	2.3823	5.5813
837.19	9.4700	- 6	2.3946	5.5934
852.17	9.2661	- 6	2.4058	5.6051
866.73	9.0737	- 6	2.4158	5.6163
880.79	8.8932	- 6	2.4247	5.6269
894.31	8.7247	- 6	2.4326	5.6370
907.22	8.5682	- 6	2.4396	5.6465
919.47	8.4240	- 6	2.4457	5.6555
931.01	8.2917	- 6	2.4510	5.6638
941.79	8.1712	- 6	2.4556	5.6715
951.77	8.0624	- 6	2.4596	5.6786
960.90	7.9651	- 6	2.4630	5.6850
969.14	7.8792	- 6	2.4658	5.6908
976.47	7.8038	- 6	2.4682	5.6959
982.85	7.7396	- 6	2.4702	5.7003
988.25	7.6863	- 6	2.4718	5.7040
992.65	7.6428	- 6	2.4730	5.7070
996.03	7.6104	- 6	2.4740	5.7093
998.38	7.5875	- 6	2.4746	5.7109
999.69	7.5748	- 6	2.4750	5.7118

 \dagger Gaussian frequencies, interval: 500-1000 kc.

Table 16

 $\sigma = 0.002$ $\epsilon_2 = 15$ $\alpha = 0.85$

d = 621 miles

d = 1000 miles

\dagger f, kc	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$
0.030725	7.9832	-11	2.4037	2.2340
0.16175	1.8503	-10	4.3915	-1 1.1157
0.39689	4.5571	-10	2.8455	-1 2.6077
0.73521	8.2296	-10	2.6818	-1 4.5486
1.1753	1.2779	-9	2.8658	-1 6.8413
1.7153	1.8106	-9	3.1942	-1 9.3983
2.3530	2.4112	-9	3.6026	-1 1.2145
3.0857	3.0705	-9	4.0648	-1 1.5017
3.9103	3.7793	-9	4.5683	-1 1.7960
4.8233	4.5294	-9	5.1060	-1 2.0930
5.8210	5.3126	-9	5.6736	-1 2.3888
6.8991	6.1212	-9	6.2678	-1 2.6803
8.0532	6.9481	-9	6.8859	-1 2.9646
9.2783	7.7863	-9	7.5256	-1 3.2395
10.569	8.6291	-9	8.1847	-1 3.5031
11.921	9.4704	-9	8.8610	-1 3.7538
13.327	1.0304	-8	9.5523	-1 3.9902
14.783	1.1125	-8	1.0256	4.2111
16.281	1.1928	-8	1.0971	4.4158
17.816	1.2708	-8	1.1694	4.6035
19.381	1.3461	-8	1.2422	4.7738
20.969	1.4182	-8	1.3153	4.9264
22.575	1.4870	-8	1.3886	5.0613
24.190	1.5520	-8	1.4616	5.1788
25.810	1.6132	-8	1.5342	5.2791
27.425	1.6702	-8	1.6060	5.3629
29.031	1.7231	-8	1.6770	5.4308
30.619	1.7717	-8	1.7467	5.4838
32.184	1.8161	-8	1.8149	5.5228
33.719	1.8563	-8	1.8814	5.5491
35.217	1.8924	-8	1.9460	5.5638
36.673	1.9246	-8	2.0084	5.5683
38.079	1.9530	-8	2.0683	5.5639
39.431	1.9780	-8	2.1257	5.5519
40.722	1.9996	-8	2.1802	5.5338
41.947	2.0182	-8	2.2318	5.5109
43.101	2.0340	-8	2.2801	5.4843
44.179	2.0473	-8	2.3251	5.4554
45.177	2.0584	-8	2.3666	5.4252
46.090	2.0675	-8	2.4045	5.3949
46.914	2.0749	-8	2.4386	5.3653
47.647	2.0809	-8	2.4688	5.3374
48.285	2.0855	-8	2.4950	5.3119
48.825	2.0891	-8	2.5171	5.2894
49.265	2.0918	-8	2.5352	5.2705
49.603	2.0937	-8	2.5490	5.2557
49.838	2.0950	-8	2.5586	5.2452
49.969	2.0957	-8	2.5640	5.2392

 \dagger Gaussian frequencies, interval: 0-50 kc.

Table 17

 $\sigma = 0.002$ $\epsilon_2 = 15$ $\alpha = 0.85$

d = 621 miles

d = 1000 miles

f, kc	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$
50.277	2.0972	- 8	2.5765	5.2252
51.456	2.1021	- 8	2.6245	5.1692
53.572	2.1073	- 8	2.7102	5.0608
56.617	2.107	- 8	2.832	4.889
60.578	2.093	- 8	2.989	4.643
65.438	2.059	- 8	3.179	4.314
71.177	1.995	- 8	3.397	3.905
77.771	1.898	- 8	3.642	3.425
85.193	1.766	- 8	3.908	2.900
93.410	1.60	- 8	4.19	2.36
102.39	1.41	- 8	4.48	1.84
112.09	1.20	- 8	4.78	1.37
122.48	9.98	- 9	5.07	9.78
133.50	8.01	- 9	5.34	6.69
145.12	4.89	- 9	5.11	2.79
157.29	4.42	- 9	5.65	2.46
169.95	3.60	- 9	6.03	1.81
183.05	2.80	- 9	2.99	- 2
196.53	2.13	- 9	2.51	- 1
210.34	1.63	- 9	4.35	- 1
224.43	1.24	- 9	5.85	- 1
238.72	9.56	- 10	7.12	- 1
253.17	7.49	- 10	8.25	- 1
267.71	5.91	- 10	9.23	- 1
282.29	4.73	- 10	1.01	8.26
296.83	3.83	- 10	1.09	6.02
311.28	3.14	- 10	1.16	4.46
325.57	2.60	- 10	1.23	3.36
339.66	2.18	- 10	1.29	2.58
353.47	1.85	- 10	1.34	2.01
366.95	1.58	- 10	1.39	1.59
380.05	1.37	- 10	1.44	1.28
392.71	1.20	- 10	1.49	1.04
404.88	1.06	- 10	1.53	8.61
416.50	9.39	- 11	1.56	7.22
427.52	8.43	- 11	1.60	6.13
437.91	7.64	- 11	1.63	5.28
447.61	6.98	- 11	1.66	4.60
456.59	6.43	- 11	1.69	4.06
464.81	5.97	- 11	1.71	3.63
472.23	5.59	- 11	1.73	3.29
478.82	5.28	- 11	1.75	3.02
484.56	5.03	- 11	1.76	2.80
489.42	4.82	- 11	1.78	2.63
493.38	4.66	- 11	1.79	2.50
496.43	4.55	- 11	1.80	2.40
498.54	4.47	- 11	1.80	2.34
499.72	4.42	- 11	1.81	2.30

† Gaussian frequencies, interval: 50-500 kc.

Table 18

 $\sigma = 0.002$ $\epsilon_2 = 15$ $\alpha = 0.85$

[†] f, kc	d = 621 miles			d = 1000 miles		
	E _r	arg E _r	E _r	arg E _r		
500.31	4.40	-11	1.81	2.29	-13	5.51
501.62	4.36	-11	1.81	2.25	-13	5.52
503.97	4.27	-11	1.82	2.18	-13	5.53
507.35	4.16	-11	1.83	2.09	-13	5.54
511.75	4.01	-11	1.84	1.98	-13	5.56
517.15	3.84	-11	1.85	1.86	-13	5.59
523.53	3.65	-11	1.87	1.72	-13	5.61
530.86	3.44	-11	1.89	1.57	-13	5.64
539.10	3.23	-11	1.91	1.43	-13	5.68
548.23	3.01	-11	1.93	1.28	-13	5.71
558.21	2.79	-11	1.95	1.14	-13	5.75
568.99	2.58	-11	1.98	1.01	-13	5.80
580.53	2.37	-11	2.01	8.90	-14	5.84
592.78	2.17	-11	2.04	7.78	-14	5.89
605.69	1.98	-11	2.07	6.78	-14	5.94
619.21	1.81	-11	2.10	5.88	-14	5.99
633.27	1.646	-11	2.128	5.087	-14	6.041
647.83	1.495	-11	2.160	4.390	-14	6.094
662.81	1.357	-11	2.192	3.784	-14	6.148
678.16	1.232	-11	2.224	3.260	-14	6.202
693.81	1.118	-11	2.256	2.808	-14	6.257
709.69	1.015	-11	2.289	2.420	-14	2.829
725.75	9.2218	-12	2.3210	2.0887	-14	8.2694
741.90	8.3909	-12	2.3529	1.8059	-14	1.3668
758.10	7.6471	-12	2.3843	1.5650	-14	1.9005
774.25	6.9824	-12	2.4152	1.3602	-14	2.4260
790.31	6.3895	-12	2.4455	1.1860	-14	2.9414
806.19	5.8614	-12	2.4750	1.0380	-14	3.4450
821.84	5.3915	-12	2.5037	9.1215	-15	3.9351
837.19	4.9738	-12	2.5315	8.0516	-15	4.4103
852.17	4.6029	-12	2.5583	7.1412	-15	4.8689
866.73	4.2739	-12	2.5840	6.3661	-15	5.3097
880.79	3.9823	-12	2.6085	5.7056	-15	5.7314
894.31	3.7243	-12	2.6319	5.1425	-15	6.1327
907.22	3.4962	-12	2.6540	4.6622	-15	6.5126
919.47	3.2950	-12	2.6747	4.2524	-15	6.8700
931.01	3.1181	-12	2.6941	3.9029	-15	7.2040
941.79	2.9629	-12	2.7121	3.6052	-15	7.5138
951.77	2.8274	-12	2.7286	3.3523	-15	7.7985
960.90	2.7099	-12	2.7436	3.1380	-15	8.0575
969.14	2.6087	-12	2.7570	2.9576	-15	8.2901
976.47	2.5225	-12	2.7689	2.8070	-15	8.4958
982.85	2.4503	-12	2.7793	2.6829	-15	8.6740
988.25	2.3910	-12	2.7879	2.5826	-15	8.8244
992.65	2.3440	-12	2.7950	2.5039	-15	8.9466
996.03	2.3085	-12	2.8004	2.4452	-15	9.0403
998.38	2.2843	-12	2.8042	2.4054	-15	9.1053
999.69	2.2709	-12	2.8063	2.3835	-15	9.1415

† Gaussian frequencies, interval: 500-1000 kc.

Table 19

 $\sigma = 5$ $\epsilon_2 = 80$ $\alpha = 0.85$

d = 12.49 miles

d = 329 miles

\dagger f, kc	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$
0.030725	1.1456	- 5	3.01286	5.08965
0.16175	2.01713	- 6	3.0732	3.03337
0.39689	8.07482	- 7	2.09712	8.08928
0.73521	4.05756	- 7	2.08115	8.08928
1.0753	2.07037	- 7	2.05609	2.06294
1.07153	1.07779	- 7	2.01547	3.07986
2.03530	1.04837	- 7	1.05879	5.01536
3.00857	1.06799	- 7	1.00826	6.06823
3.09103	2.01414	- 7	7.06563	- 1
4.08233	2.07248	- 7	5.07613	- 1
5.08210	3.03776	- 7	4.05522	- 1
6.08991	4.00820	- 7	3.07253	- 1
8.00532	4.08309	- 7	3.01282	- 1
9.02783	5.06204	- 7	2.06791	- 1
10.0569	6.04476	- 7	2.03307	- 1
11.0921	7.03095	- 7	2.00540	- 1
13.0327	8.02030	- 7	1.08299	- 1
14.0783	9.01250	- 7	1.06457	- 1
16.0281	1.00072	- 6	1.04922	- 1
17.0816	1.01041	- 6	1.03630	- 1
19.0381	1.02027	- 6	1.02533	- 1
20.0969	1.03026	- 6	1.01593	- 1
22.0575	1.04036	- 6	1.00783	- 1
24.0190	1.05051	- 6	1.00080	- 1
25.0810	1.06068	- 6	9.04675	- 2
27.0425	1.07082	- 6	8.09311	- 2
29.0031	1.08089	- 6	8.04596	- 2
30.0619	1.09085	- 6	8.00438	- 2
32.0184	2.00066	- 6	7.06761	- 2
33.0719	2.01028	- 6	7.03502	- 2
35.0217	2.01967	- 6	7.00608	- 2
36.0673	2.02879	- 6	6.08035	- 2
38.0079	2.03760	- 6	6.05747	- 2
39.0431	2.04606	- 6	6.03711	- 2
40.0722	2.05415	- 6	6.01900	- 2
41.0947	2.06182	- 6	6.00292	- 2
43.101	2.06905	- 6	5.08867	- 2
44.0179	2.07580	- 6	5.07608	- 2
45.0177	2.08204	- 6	5.06501	- 2
46.0090	2.08776	- 6	5.05533	- 2
46.0914	2.09292	- 6	5.04694	- 2
47.0647	2.09750	- 6	5.03975	- 2
48.0285	3.00150	- 6	5.03369	- 2
48.0825	3.00488	- 6	5.02869	- 2
49.0265	3.00763	- 6	5.02471	- 2
49.0603	3.00975	- 6	5.02170	- 2
49.0838	3.01122	- 6	5.01963	- 2
49.0969	3.01204	- 6	5.01849	- 2

 \dagger Gaussian frequencies, interval: 0-50 kc.

Table 20

$$\sigma = 5 \quad \epsilon_2 = 80 \quad \alpha = 0.85$$

d = 12.49 miles

d = 329 miles

\dagger f, kc	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$
50.277	3.1396	- 6	5.1584	- 2
51.456	3.2134	- 6	5.0599	- 2
53.572	3.3459	- 6	4.8952	- 2
56.617	3.5364	- 6	4.6822	- 2
60.578	3.7842	- 6	4.4412	- 2
65.438	4.0883	- 6	4.1912	- 2
71.177	4.4473	- 6	3.9474	- 2
77.771	4.8597	- 6	3.7207	- 2
85.193	5.3239	- 6	3.5182	- 2
93.410	5.8378	- 6	3.3434	- 2
102.39	6.3993	- 6	3.1974	- 2
112.09	7.0060	- 6	3.0799	- 2
122.48	7.6554	- 6	2.9894	- 2
133.50	8.3448	- 6	2.9239	- 2
145.12	9.0713	- 6	2.8813	- 2
157.29	9.8318	- 6	2.8592	- 2
169.95	1.0623	- 5	2.8554	- 2
183.05	1.1442	- 5	2.8679	- 2
196.53	1.2285	- 5	2.8947	- 2
210.34	1.3149	- 5	2.9340	- 2
224.43	1.4029	- 5	2.9841	- 2
238.72	1.4923	- 5	3.0435	- 2
253.17	1.5826	- 5	3.1108	- 2
267.71	1.6735	- 5	3.1847	- 2
282.29	1.7646	- 5	3.2640	- 2
296.83	1.8554	- 5	3.3477	- 2
311.28	1.9457	- 5	3.4346	- 2
325.57	2.0351	- 5	3.5239	- 2
339.66	2.1231	- 5	3.6146	- 2
353.47	2.2094	- 5	3.7058	- 2
366.95	2.2937	- 5	3.7969	- 2
380.05	2.3756	- 5	3.8871	- 2
392.71	2.4547	- 5	3.9756	- 2
404.88	2.5307	- 5	4.0619	- 2
416.50	2.6033	- 5	4.1453	- 2
427.52	2.6722	- 5	4.2252	- 2
437.91	2.7371	- 5	4.3012	- 2
447.61	2.7977	- 5	4.3728	- 2
456.59	2.8538	- 5	4.4394	- 2
464.81	2.9051	- 5	4.5008	- 2
472.23	2.9515	- 5	4.5565	- 2
478.82	2.9927	- 5	4.6062	- 2
484.56	3.0286	- 5	4.6496	- 2
489.42	3.0589	- 5	4.6864	- 2
493.38	3.0837	- 5	4.7165	- 2
496.43	3.1027	- 5	4.7397	- 2
498.54	3.1159	- 5	4.7558	- 2
499.72	3.1233	- 5	4.7648	- 2
			3.8943	- 7
			3.9061	- 7
			3.9142	- 7
			3.9187	- 7

 \dagger Gaussian frequencies, interval: 50-500 kc.

Table 21

$\sigma = 5$	$\epsilon_2 = 80$	$\alpha = 0.85$	$d = 12.49 \text{ miles}$		$d = 329 \text{ miles}$	
f, kc	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$
500.31	3.1269	- 5	4.7693	- 2	3.9210	- 7
501.62	3.1351	- 5	4.7793	- 2	3.9260	- 7
503.97	3.1498	- 5	4.7973	- 2	3.9350	- 7
507.35	3.1709	- 5	4.8232	- 2	3.9478	- 7
511.75	3.1984	- 5	4.8570	- 2	3.9644	- 7
517.15	3.2321	- 5	4.8985	- 2	3.9845	- 7
523.53	3.2720	- 5	4.9476	- 2	4.0080	- 7
530.86	3.3177	- 5	5.0043	- 2	4.0347	- 7
539.10	3.3692	- 5	5.0682	- 2	4.0644	- 7
548.23	3.4263	- 5	5.1392	- 2	4.0966	- 7
558.21	3.4886	- 5	5.2171	- 2	4.1313	- 7
568.99	3.5559	- 5	5.3016	- 2	4.1681	- 7
580.53	3.6280	- 5	5.3924	- 2	4.2066	- 7
592.78	3.7045	- 5	5.4891	- 2	4.2467	- 7
605.69	3.7851	- 5	5.5914	- 2	4.2881	- 7
619.21	3.8695	- 5	5.6989	- 2	4.3303	- 7
633.27	3.9573	- 5	5.8111	- 2	4.3733	- 7
647.83	4.0482	- 5	5.9276	- 2	4.4166	- 7
662.81	4.1418	- 5	6.0479	- 2	4.4602	- 7
678.16	4.2376	- 5	6.1716	- 2	4.5036	- 7
693.81	4.3353	- 5	6.2980	- 2	4.5468	- 7
709.69	4.4344	- 5	6.4267	- 2	4.5895	- 7
725.75	4.5346	- 5	6.5571	- 2	4.6315	- 7
741.90	4.6355	- 5	6.6887	- 2	4.6726	- 7
758.10	4.7365	- 5	6.8208	- 2	4.7128	- 7
774.25	4.8373	- 5	6.9529	- 2	4.7518	- 7
790.31	4.9375	- 5	7.0845	- 2	4.7896	- 7
806.19	5.0366	- 5	7.2149	- 2	4.8260	- 7
821.84	5.1342	- 5	7.3436	- 2	4.8610	- 7
837.19	5.2300	- 5	7.4701	- 2	4.8944	- 7
852.17	5.3235	- 5	7.5937	- 2	4.9263	- 7
866.73	5.4142	- 5	7.7139	- 2	4.9566	- 7
880.79	5.5019	- 5	7.8303	- 2	4.9852	- 7
894.31	5.5862	- 5	7.9422	- 2	5.0120	- 7
907.22	5.6667	- 5	8.0492	- 2	5.0372	- 7
919.47	5.7431	- 5	8.1509	- 2	5.0605	- 7
931.01	5.8151	- 5	8.2467	- 2	5.0821	- 7
941.79	5.8823	- 5	8.3363	- 2	5.1020	- 7
951.77	5.9445	- 5	8.4193	- 2	5.1200	- 7
960.90	6.0014	- 5	8.4953	- 2	5.1363	- 7
969.14	6.0528	- 5	8.5640	- 2	5.1508	- 7
976.47	6.0985	- 5	8.6250	- 2	5.1635	- 7
982.85	6.1382	- 5	8.6782	- 2	5.1745	- 7
988.25	6.1719	- 5	8.7232	- 2	5.1837	- 7
992.65	6.1993	- 5	8.7599	- 2	5.1911	- 7
996.03	6.2204	- 5	8.7881	- 2	5.1968	- 7
998.38	6.2351	- 5	8.8077	- 2	5.2007	- 7
999.69	6.2432	- 5	8.8187	- 2	5.2029	- 7

† Gaussian frequencies, interval: 500-1000 kc.

Table 22

 $\sigma = 5$ $\epsilon_2 = 80$ $\alpha = 0.85$

\dagger $f, \text{ kc}$	d = 621 miles			d = 1000 miles		
	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$		
0.030725	7.9832	-11	2.4028		2.2340	-11
0.16175	1.8503	-10	4.3432	-1	1.1156	-10
0.39689	4.5565	-10	2.7263	-1	2.6068	-10
0.73521	8.2271	-10	2.4599	-1	4.5449	-10
1.1753	1.2772	-9	2.5095	-1	6.8306	-10
1.7153	1.8089	-9	2.6718	-1	9.3739	-10
2.3530	2.4080	-9	2.8827	-1	1.2097	-9
3.0857	3.0649	-9	3.1166	-1	1.4934	-9
3.9103	3.7705	-9	3.3616	-1	1.7829	-9
4.8233	4.5126	-9	3.6220	-1	2.0735	-9
5.8210	5.2907	-9	3.8692	-1	2.3617	-9
6.8991	6.0945	-9	4.1166	-1	2.6444	-9
8.0532	6.9170	-9	4.3623	-1	2.9191	-9
9.2783	7.7522	-9	4.6054	-1	3.1840	-9
10.569	8.5944	-9	4.8450	-1	3.4377	-9
11.921	9.4385	-9	5.0804	-1	3.6794	-9
13.327	1.0280	-8	5.3111	-1	3.9083	-9
14.783	1.1117	-8	5.5375	-1	4.1241	-9
16.281	1.1941	-8	5.7578	-1	4.3268	-9
17.816	1.2751	-8	5.9725	-1	4.5163	-9
19.381	1.3545	-8	6.1812	-1	4.6930	-9
20.969	1.4320	-8	6.3839	-1	4.8570	-9
22.575	1.5074	-8	6.5804	-1	5.0089	-9
24.190	1.5806	-8	6.7704	-1	5.1491	-9
25.810	1.6512	-8	6.9540	-1	5.2782	-9
27.425	1.7194	-8	7.1309	-1	5.3967	-9
29.031	1.7848	-8	7.3011	-1	5.5052	-9
30.619	1.8474	-8	7.4643	-1	5.6042	-9
32.184	1.9072	-8	7.6207	-1	5.6945	-9
33.719	1.9641	-8	7.7699	-1	5.7764	-9
35.217	2.0181	-8	7.9120	-1	5.8507	-9
36.673	2.0691	-8	8.0468	-1	5.9178	-9
38.079	2.1171	-8	8.1742	-1	5.9783	-9
39.431	2.1621	-8	8.2942	-1	6.0326	-9
40.722	2.2041	-8	8.4068	-1	6.0812	-9
41.947	2.2430	-8	8.5117	-1	6.1246	-9
43.101	2.2790	-8	8.6090	-1	6.1632	-9
44.179	2.3119	-8	8.6986	-1	6.1972	-9
45.177	2.3419	-8	8.7804	-1	6.2272	-9
46.090	2.3688	-8	8.8544	-1	6.2533	-9
46.914	2.3929	-8	8.9205	-1	6.2758	-9
47.647	2.4139	-8	8.9787	-1	6.2951	-9
48.285	2.4321	-8	9.0290	-1	6.3113	-9
48.825	2.4473	-8	9.0713	-1	6.3246	-9
49.265	2.4596	-8	9.1055	-1	6.3352	-9
49.603	2.4690	-8	9.1318	-1	6.3432	-9
49.838	2.4755	-8	9.1499	-1	6.3486	-9
49.969	2.4791	-8	9.1600	-1	6.3516	-9

\dagger Gaussian frequencies, interval: 0-50 kc.

Table 23

$$\sigma = 5 \quad \epsilon_2 = 80 \quad \alpha = 0.85$$

d = 621 miles

d = 1000 miles

[†] f, kc	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$
50.277	2.4875	- 8	9.1836	- 1
51.456	2.5195	- 8	9.2736	- 1
53.572	2.5755	- 8	9.4321	- 1
56.617	2.6529	- 8	9.6543	- 1
60.578	2.7483	- 8	9.9335	- 1
65.438	2.8580	- 8	1.0263	
71.177	2.9782	- 8	1.0634	
77.771	3.1050	- 8	1.1041	
85.193	3.2350	- 8	1.1477	
93.410	3.3652	- 8	1.1936	
102.39	3.4930	- 8	1.2413	
112.09	3.6163	- 8	1.2904	
122.48	3.7336	- 8	1.3405	
133.50	3.8437	- 8	1.3913	
145.12	3.9459	- 8	1.4425	
157.29	4.0396	- 8	1.4939	
169.95	4.1247	- 8	1.5453	
183.05	4.2012	- 8	1.5964	
196.53	4.2692	- 8	1.6472	
210.34	4.3291	- 8	1.6975	
224.43	4.3813	- 8	1.7472	
238.72	4.4263	- 8	1.7961	
253.17	4.4645	- 8	1.8442	
267.71	4.4964	- 8	1.8913	
282.29	4.5227	- 8	1.9373	
296.83	4.5439	- 8	1.9822	
311.28	4.5605	- 8	2.0258	
325.57	4.5730	- 8	2.0682	
339.66	4.5819	- 8	2.1091	
353.47	4.5878	- 8	2.1485	
366.95	4.5909	- 8	2.1864	
380.05	4.5918	- 8	2.2227	
392.71	4.5908	- 8	2.2572	
404.88	4.5882	- 8	2.2900	
416.50	4.5845	- 8	2.3209	
427.52	4.5798	- 8	2.3500	
437.91	4.5745	- 8	2.3770	
447.61	4.5689	- 8	2.4021	
456.59	4.5630	- 8	2.4251	
464.81	4.5572	- 8	2.4461	
472.23	4.5516	- 8	2.4648	
478.82	4.5463	- 8	2.4814	
484.56	4.5415	- 8	2.4958	
489.42	4.5373	- 8	2.5079	
493.38	4.5338	- 8	2.5177	
496.43	4.5311	- 8	2.5253	
498.54	4.5291	- 8	2.5305	
499.72	4.5280	- 8	2.5334	
			3.2665	- 9
			4.1937	

[†] Gaussian frequencies, interval: 50-500 kc.

Table 24

$\sigma = 5$	$\epsilon_2 = 80$	$\alpha = 0.85$	$d = 621 \text{ miles}$		$d = 1000 \text{ miles}$	
$f, \text{ kc}^\dagger$	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$
500.31	4.5275	- 8	2.5349		3.2632	- 9
501.62	4.5262	- 8	2.5381		3.2558	- 9
503.97	4.5240	- 8	2.5439		3.2425	- 9
507.35	4.5208	- 8	2.5522		3.2236	- 9
511.75	4.5165	- 8	2.5630		3.1992	- 9
517.15	4.5111	- 8	2.5762		3.1696	- 9
523.53	4.5045	- 8	2.5917		3.1352	- 9
530.86	4.4968	- 8	2.6094		3.0962	- 9
539.10	4.4879	- 8	2.6293		3.0530	- 9
548.23	4.4776	- 8	2.6511		3.0062	- 9
558.21	4.4661	- 8	2.6748		2.9562	- 9
568.99	4.4533	- 8	2.7003		2.9033	- 9
580.53	4.4392	- 8	2.7274		2.8482	- 9
592.78	4.4238	- 8	2.7560		2.7911	- 9
605.69	4.4072	- 8	2.7858		2.7327	- 9
619.21	4.3893	- 8	2.8168		2.6732	- 9
633.27	4.3703	- 8	2.8489		2.6132	- 9
647.83	4.3502	- 8	2.8818		2.5529	- 9
662.81	4.3291	- 8	2.9154		2.4929	- 9
678.16	4.3072	- 8	2.9496		2.4333	- 9
693.81	4.2844	- 8	2.9842		2.3744	- 9
709.69	4.2610	- 8	3.0191		2.3166	- 9
725.75	4.2371	- 8	3.0541		2.2601	- 9
741.90	4.2128	- 8	3.0890		2.2051	- 9
758.10	4.1882	- 8	3.1238		2.1517	- 9
774.25	4.1635	- 8	3.1583		2.1001	- 9
790.31	4.1387	- 8	3.1924		2.0505	- 9
806.19	4.1141	- 8	3.2259		2.0029	- 9
821.84	4.0898	- 8	3.2587		1.9575	- 9
837.19	4.0658	- 8	3.2907		1.9142	- 9
852.17	4.0424	- 8	3.3218		1.8732	- 9
866.73	4.0196	- 8	3.3518		1.8344	- 9
880.79	3.9975	- 8	3.3807		1.7979	- 9
894.31	3.9762	- 8	3.4084		1.7638	- 9
907.22	3.9560	- 8	3.4347		1.7319	- 9
919.47	3.9367	- 8	3.4595		1.7024	- 9
931.01	3.9186	- 8	3.4828		1.6752	- 9
941.79	3.9016	- 8	3.5046		1.6503	- 9
951.77	3.8860	- 8	3.5246		1.6277	- 9
960.90	3.8717	- 8	3.5429		1.6073	- 9
969.14	3.8587	- 8	3.5594		1.5892	- 9
976.47	3.8473	- 8	3.5740		1.5734	- 9
982.85	3.8373	- 8	3.5867		1.5597	- 9
988.25	3.8288	- 8	3.5974		1.5483	- 9
992.65	3.8220	- 8	3.6061		1.5391	- 9
996.03	3.8167	- 8	3.6128		1.5320	- 9
998.38	3.8130	- 8	3.6175		1.5271	- 9
999.69	3.8110	- 8	3.6201		1.5244	- 9

Table 25

$f = 153.5 \text{ kc}$

d, miles	$\sigma = 0.001$			$\sigma = 0.002$		
	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$
50	1.33	- 6	1.75	1.80	- 6	1.32
60	1.00	- 6	1.90	1.41	- 6	1.45
70	7.77	- 7	2.04	1.15	- 6	1.56
80	6.17	- 7	2.17	9.48	- 7	1.67
100	4.08	- 7	2.39	6.77	- 7	1.86
200	8.68	- 8	3.22	1.91	- 7	2.66
300	2.77	- 8	3.87	7.23	- 8	3.34
400	1.06	- 8	4.49	3.09	- 8	3.98
500	4.44	- 9	5.12	1.42	- 8	4.61
600	1.94	- 9	5.77	6.74	- 9	5.24
$\sigma = 0.003$						
	$\epsilon_2 = 15$			$\sigma = 0.004$		
	$\alpha^2 = 0.75$			$\epsilon_2 = 15$		
				$\alpha^2 = 0.75$		
50	1.96	- 6	1.10	2.04	- 6	9.62
60	1.56	- 6	1.21	1.65	- 6	1.06
70	1.29	- 6	1.31	1.36	- 6	1.15
80	1.08	- 6	1.40	1.15	- 6	1.24
100	7.93	- 6	1.58	8.60	- 7	1.40
200	2.57	- 7	2.34	2.99	- 7	2.11
300	1.10	- 7	3.02	1.36	- 7	2.75
400	5.23	- 8	3.67	6.84	- 8	3.38
500	2.63	- 8	4.32	3.63	- 8	4.01
600	1.37	- 8	4.97	1.98	- 8	4.63
$\sigma = 0.005$						
	$\epsilon_2 = 15$			$\sigma = 0.006$		
	$\alpha^2 = 0.75$			$\epsilon_2 = 15$		
				$\alpha^2 = 0.75$		
50	2.10	- 6	8.68	- 1	2.133	- 6
60	1.70	- 6	9.57	- 1	1.732	- 6
70	1.41	- 6	1.04		1.447	- 6
80	1.20	- 6	1.12		1.233	- 6
100	9.04	- 7	1.27		9.338	- 7
200	3.27	- 7	1.94		3.479	- 7
300	1.55	- 7	2.55		1.684	- 7
400	8.06	- 8	3.15		8.987	- 8
500	4.42	- 8	3.75		5.033	- 8
600	2.49	- 8	4.35		2.896	- 8
						- 1
						- 1
						- 1

Table 26

$f = 153.5 \text{ kc}$

d, miles	$\sigma = 0.007$		$\sigma = 0.01$		$\sigma = 0.02$		$\sigma = 5$	
	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$	$ E_r $	$\arg E_r$
50	2.159	- 6	7.436	- 1	2.208	- 6	6.310	- 1
60	1.758	- 6	8.213	- 1	1.805	- 6	6.983	- 1
70	1.471	- 6	8.948	- 1	1.517	- 6	7.623	- 1
80	1.257	- 6	9.652	- 1	1.300	- 6	8.238	- 1
100	9.559	- 7	1.099		9.968	- 7	9.415	- 1
200	3.634	- 7	1.701		3.925	- 7	1.480	
300	1.790	- 7	2.265		1.995	- 7	1.995	
400	9.711	- 8	2.823		1.114	- 7	2.507	
500	5.522	- 8	3.381		6.507	- 8	3.021	
600	3.224	- 8	3.941		3.899	- 8	3.538	
	$\epsilon^2 = 15$		$\epsilon^2 = 15$		$\epsilon^2 = 80$		$\epsilon^2 = 0.75$	
50	2.2647	- 6	4.5998	- 1	2.3175995	- 6	6.8680500	- 2
60	1.8599	- 6	5.1114	- 1	1.9110039	- 6	8.2034550	- 2
70	1.5699	- 6	5.6030	- 1	1.6192783	- 6	9.6247370	- 2
80	1.3518	- 6	6.0798	- 1	1.3994859	- 6	1.1121350	- 1
100	1.0453	- 6	7.0025	- 1	1.0897548	- 6	1.4312537	- 1
200	4.2808	- 7	1.1372		4.5842073	- 7	3.3207809	- 1
300	2.2518	- 7	1.5678		2.4498846	- 7	5.5295098	- 1
400	1.2960	- 7	2.0028		1.4212180	- 7	7.9135687	- 1
500	7.7860	- 8	2.4423		8.5620686	- 8	1.0387779	
600	4.7913	- 8	2.8847		5.2676120	- 8	1.2903433	
	$\alpha^2 = 0.75$		$\alpha^2 = 0.85$		$\alpha^2 = 0.75$		$\alpha^2 = 0.85$	
50	2.09	- 6	8.74	- 1				
60	1.69	- 6	9.65	- 1				
70	1.40	- 6	1.05					
80	1.19	- 6	1.13					
100	8.94	- 7	1.29					
200	3.18	- 7	1.98					
300	1.47	- 7	2.63					
400	7.47	- 8	3.27					
500	3.98	- 8	3.92					
600	2.18	- 8	4.56					

NATIONAL BUREAU OF STANDARDS

A. V. Astin, *Director*

THE NATIONAL BUREAU OF STANDARDS

The scope of activities of the National Bureau of Standards at its major laboratories in Washington, D.C., and Boulder, Colorado, is suggested in the following listing of the divisions and sections engaged in technical work. In general, each section carries out specialized research, development, and engineering in the field indicated by its title. A brief description of the activities, and of the resultant publications, appears on the inside of the front cover.

WASHINGTON, D.C.

Electricity and Electronics. Resistance and Reactance. Electron Devices. Electrical Instruments. Magnetic Measurements. Dielectrics. Engineering Electronics. Electronic Instrumentation. Electrochemistry.

Optics and Metrology. Photometry and Colorimetry. Photographic Technology. Length. Engineering Metrology.

Heat. Temperature Physics. Thermodynamics. Cryogenic Physics. Rheology. Molecular Kinetics. Free Radicals Research.

Atomic and Radiation Physics. Spectroscopy. Radiometry. Mass Spectrometry. Solid State Physics. Electron Physics. Atomic Physics. Neutron Physics. Radiation Theory. Radioactivity. X-rays. High Energy Radiation. Nucleonic Instrumentation. Radiological Equipment.

Chemistry. Organic Coatings. Surface Chemistry. Organic Chemistry. Analytical Chemistry. Inorganic Chemistry. Electrodeposition. Molecular Structure and Properties of Gases. Physical Chemistry. Thermochemistry. Spectrochemistry. Pure Substances.

Mechanics. Sound. Mechanical Instruments. Fluid Mechanics. Engineering Mechanics. Mass and Scale. Capacity, Density, and Fluid Meters. Combustion Controls.

Organic and Fibrous Materials. Rubber. Textiles. Paper. Leather. Testing and Specifications. Polymer Structure. Plastics. Dental Research.

Metallurgy. Thermal Metallurgy. Chemical Metallurgy. Mechanical Metallurgy. Corrosion. Metal Physics.

Mineral Products. Engineering Ceramics. Glass. Refractories. Enamelled Metals. Constitution and Microstructure.

Building Technology. Structural Engineering. Fire Protection. Air Conditioning, Heating, and Refrigeration. Floor, Roof, and Wall Coverings. Codes and Safety Standards. Heat Transfer. Concreting Materials.

Applied Mathematics. Numerical Analysis. Computation. Statistical Engineering. Mathematical Physics.

Data Processing Systems. SEAC Engineering Group. Components and Techniques. Digital Circuitry. Digital Systems. Analog Systems. Application Engineering.

• Office of Basic Instrumentation. • Office of Weights and Measures.

BOULDER, COLORADO

Cryogenic Engineering. Cryogenic Equipment. Cryogenic Processes. Properties of Materials. Gas Liquefaction.

Radio Propagation Physics. Upper Atmosphere Research. Ionospheric Research. Regular Propagation Services. Sun-Earth Relationships. VHF Research. Radio Warning Services. Airglow and Aurora. Radio Astronomy and Arctic Propagation.

Radio Propagation Engineering. Data Reduction Instrumentation. Modulation Research. Radio Noise. Tropospheric Measurements. Tropospheric Analysis. Propagation Obstacles Engineering. Radio-Meteorology. Lower Atmosphere Physics.

Radio Standards. High Frequency Electrical Standards. Radio Broadcast Service. High Frequency Impedance Standards. Electronic Calibration Center. Microwave Physics. Microwave Circuit Standards.

Radio Communication and Systems. Low Frequency and Very Low Frequency Research. High Frequency and Very High Frequency Research. Ultra High Frequency and Super High Frequency Research. Modulation Research. Antenna Research. Navigation Systems. Systems Analysis. Field Operations.

